Math-3

Lesson 2-4 Vertex Form Quadratic Equation

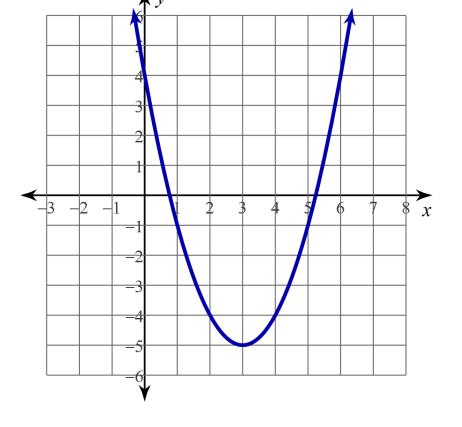
$$y = x^2 - 6x + 4$$

Can this be factored?

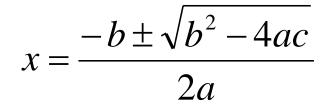
The x-intercepts are "ugly"

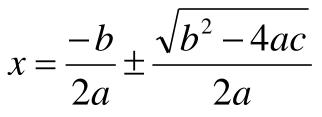
What is the vertex form equation?

$$y = (x - 3)^2 - 5$$



Does anyone remember the <u>Quadratic Formula</u>?

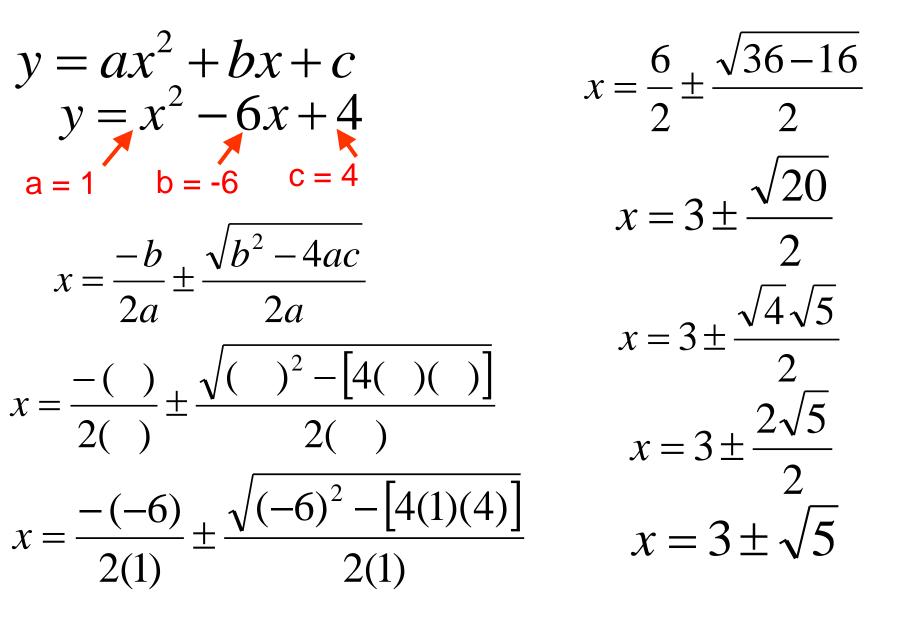




I like this version more.

What is the purpose of the formula?

The 'x' in the formula are the x-intercepts of the <u>standard form equation</u>. $y = ax^2 + bx + c$



This formula often-times results in "<u>ugly</u>" calculations where students make mistakes.

Standard Form Equation $y = x^2 - 6x + 4$

Vertex Form Equation

$$y = (x-3)^2 - 5$$

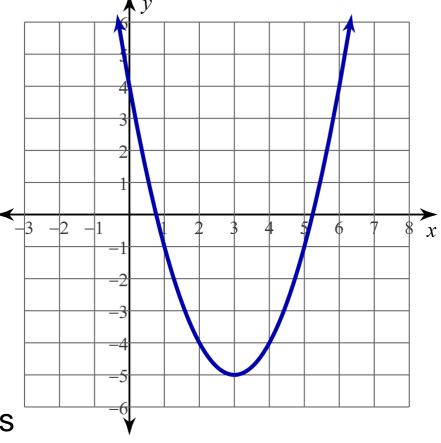
The x-intercepts that came from the quadratic formula were:

$$x = 3 \pm \sqrt{5}$$

How could you get the x-intercepts from the <u>vertex form equation</u>?

Set 'y' to zero. Isolate the square, "undo" the square.

$$\begin{array}{ll} 0 = (x-3)^2 - 5 & \pm \sqrt{5} = x - 3 \\ 5 = (x-3)^2 & x = 3 \pm \sqrt{5} \end{array}$$



Find the X-intercepts from the Vertex Form Equations

$$y = -2(x-3)^{2} + 4$$
 Set $y = 0$ (y-value of an x-int. is 0)

$$0 = -2(x-3)^{2} + 4$$
 Subtract 4 (left/right)

$$-4 = -2(x-3)^{2}$$
 Divide by -2 (left/right)

$$2 = (x-3)^{2}$$

$$2 = (_)^{2}$$
 What number, squared, equals 2?

$$2 = (\sqrt{2})^{2}$$
 $2 = (-\sqrt{2})^{2}$

$$\pm \sqrt{2} = x - 3$$
 Add 3 (left/right)

$$x = 3 \pm \sqrt{2}$$

Find the X-intercepts from the Vertex Form Equations

$$y = (x - 5)^2$$
 $y = -2(x - 3)^2 + 4$

$$y = -(x+2)^2 + 5$$

What have we learned?

1. The quadratic formula can give us x-intercepts (only if you have the *standard form equation*).

There are a lot of numbers and calculations. You can easily make a mistake.

2. If you "isolate the square, undo the square" on the <u>vertex form</u> <u>equation</u>, you can also find x-intercepts.

You have to know how to simplify square roots.

$$y = (x - 2)^{2} - 12 \qquad x = 2 \pm \sqrt{4 * 3}$$

$$0 = (x - 2)^{2} - 12 \qquad x = 2 \pm \sqrt{4}\sqrt{3}$$

$$12 = (x - 2)^{2} \qquad x = 2 \pm \sqrt{4}\sqrt{3}$$

$$x = 2 \pm \sqrt{12}$$

3. You can convert <u>standard form quadratic equations</u> into <u>intercept form quadratic equations</u> by: <u>factoring</u>

$$y = 2x^2 + 16x + 24$$
 $\rightarrow y = 2(x + 6)(x + 2)$

3. You can convert *intercept form quadratic equations* into *vertex form quadratic equations* by:

a) Finding the x-coordinate of the vertex (half way between x-intercepts) x = -6, -2 Vertex: $(-4, _)$ b) Substituting the x-value into the equation to find the y-coordinate of the vertex. y = 2(-4 + 6)(-4 + 2)y = 2(2)(-2) = -8 Vertex: (-4, -8)

c) Using the VSF and the vertex to write the vertex form equation.

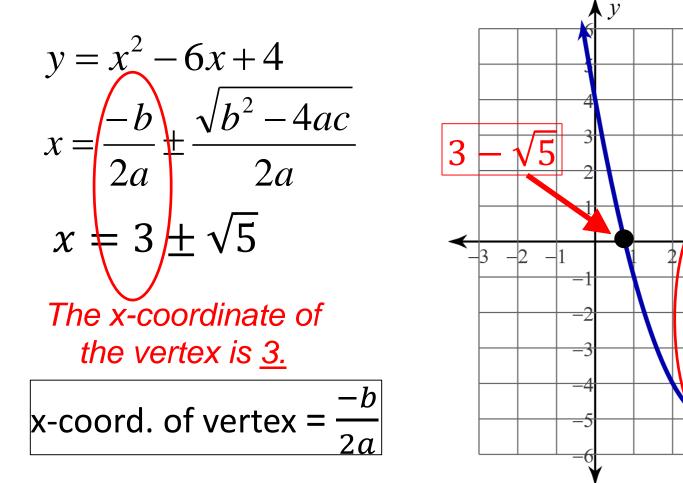
VSF = 2, Vertex:
$$(-4, -8)$$
 $y = 2(x + 4)^2 - 8$

How can we convert <u>Standard Form Quadratic Equations</u> directly into <u>Vertex form</u>? (without converting to <u>Intercept Form</u> first?)

5

x

Remember the quadratic formula gave us these x-intercepts.



What is the x-coordinate of the vertex?

$$y = 2x^2 + 16x + 24$$

$$a = 2 \qquad b = 16$$

x-coord. of vertex =
$$\frac{-b}{2a}$$

 $\frac{-b}{2a} = \frac{-16}{2(2)} = -4$

Vertex: (-4, f(-4))

What is the y-coordinate of the vertex?

$$f(-4) = 2(-4)^2 + 16(-4) + 24$$

$$f(-4) = -8$$
 Vertex: $(-4, -8)$

What is the Vertex form equation?

VSF = 2, vertex =
$$(-4, -8)$$
 $y = 2(x + 4)^2 - 8$

What is the x-coordinate of the vertex?

$$y = x^2 - 6x + 13$$
a = 1
$$b = -6$$

x-coord. of vertex =
$$\frac{-b}{2a}$$

 $\frac{-b}{2a} = \frac{-(-6)}{2(1)} = 3$

Vertex: (3, f(3))

What is the y-coordinate of the vertex?

$$f(3) = (3)^2 - 6(3) + 13$$

$$f(3) = 4$$
 Vertex: (3, 4)

What is the Vertex form equation?

VSF = 1, vertex = (3, 5)

$$y = (x - 3)^2 + 4$$

What is the x-coordinate of the vertex?

$$y = 3x^2 + 6x - 12$$
a = 3
$$b = -4$$

x-coord. of vertex =
$$\frac{-b}{2a}$$

 $\frac{-b}{2a} = \frac{-(6)}{2(3)} = -1$

Vertex: (-1, f(-1))

What is the y-coordinate of the vertex?

$$f(-1) = 3(-1)^2 + 6(-1) - 12$$

$$f(-1) = -15$$
 Vertex: $(-1, -15)$

What is the Vertex form equation?

VSF = 3, vertex = (-1, -15) $y = 3(x + 1)^2 - 15$

We have converted the following standard form equations into vertex form. What are the x-intercepts of the following equations?

$$y = 2x^2 + 16x + 24 \rightarrow y = 2(x+4)^2 - 8$$

$$y = x^2 - 6x + 13$$
 \rightarrow $y = (x - 3)^2 + 4$

$$y = 3x^2 - 6x - 12$$
 $y = 3(x + 1)^2 - 15$

Convert the following *non-factorable* standard form equations into vertex form. Find the zeroes.

$$y = x^2 - 2x - 12$$

$$y = x^2 + 20x + 99$$

$$y = x^2 - 14x + 50$$