Math-3a

Lesson 11-4
Sampling for Statistical Studies
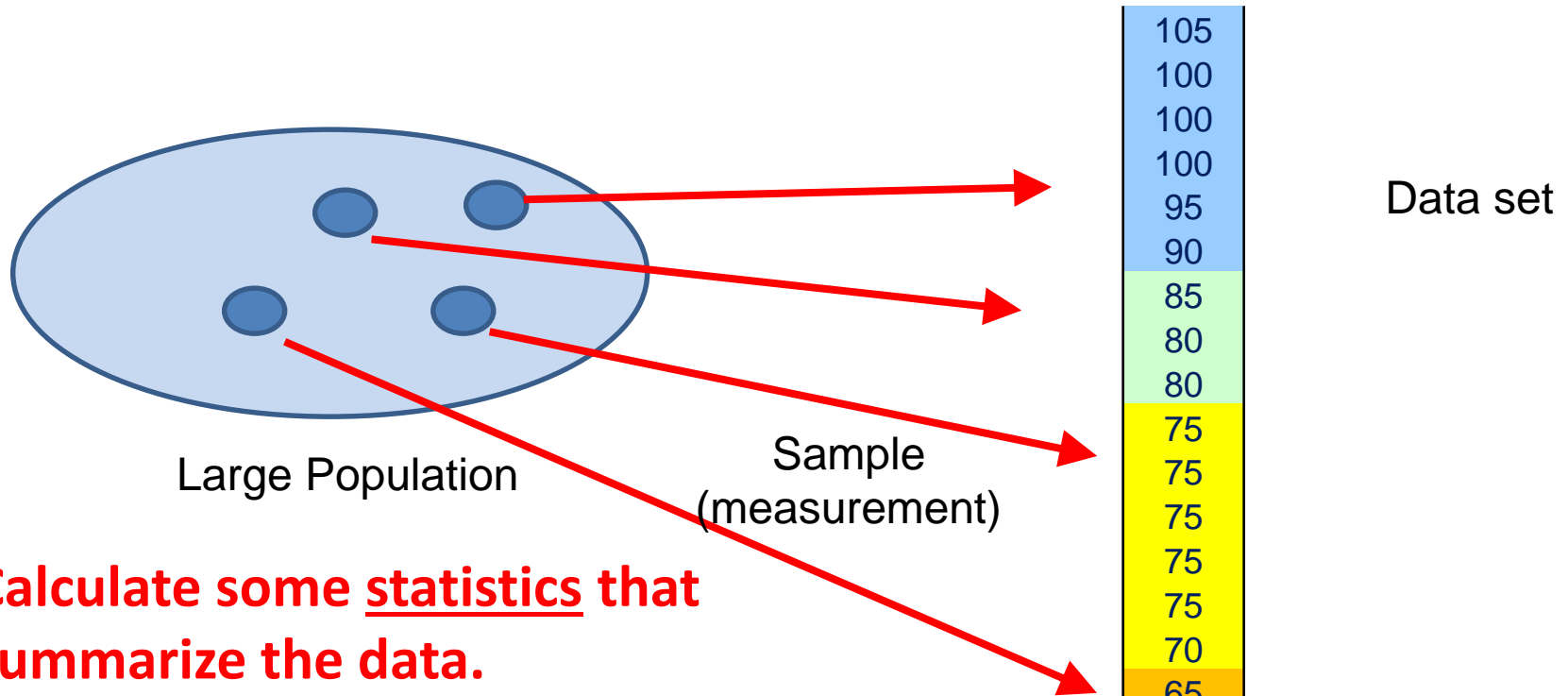(how we obtain the "numbers")

Quiz

1. What portion of the data is between 1 and 3 standard deviations above the mean of the data?

2. Danny's math score: 78, class mean math score: 84, SDEV = 3

    Danny's science score: 65, class mean

    science score: 80, SDEV = 15 On which test

    did Danny do "better" on (relative to his peers)?

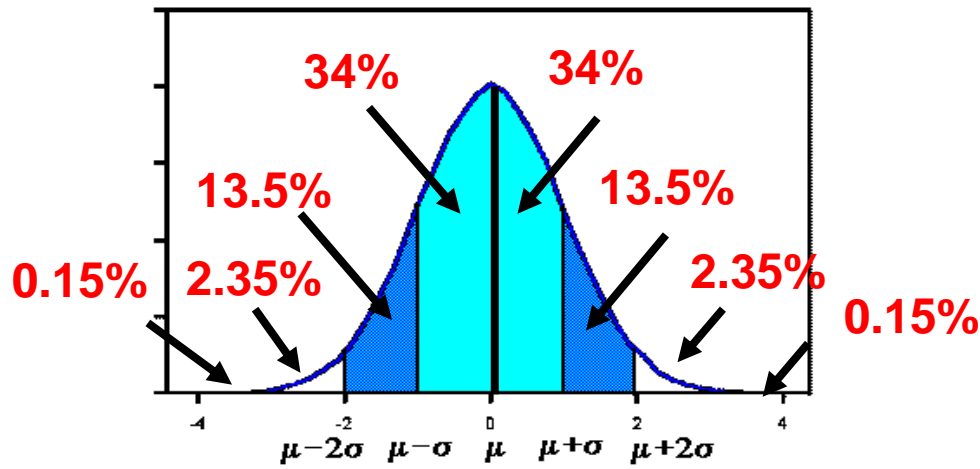3. Explain your answer to problem 3.

Quiz Problem 4.

What are the 3 types of Statistical studies and what is the purpose of each?

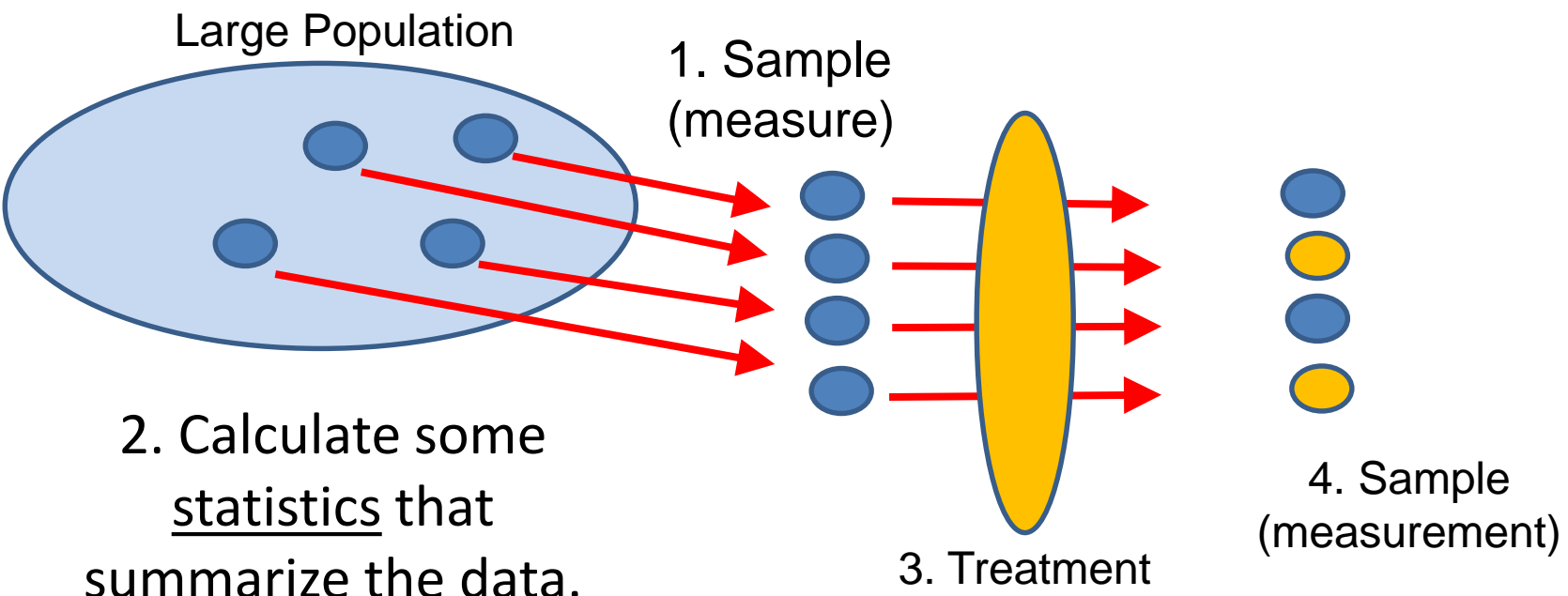| Study Type	Purpose?
Sample	Find a statistic for the population
Experiment	Is a treatment effective?
Observational	Is there a correlation between parameters in the population?

1. **"Sample Study"** - The purpose of a sample study is to *estimate* a certain parameter of a population.

Large Population

Sample (measurement)

Data set

Calculate some statistics that summarize the data.

Data set values:
105, 100, 100, 100, 95, 90, 85, 80, 80, 75, 75, 75, 75, 75, 75, 70, 65, 55, 50, 50, 50, 45, 35

34%   34%

13.5%   13.5%

0.15%   2.35%   2.35%   0.15%

$\mu-2\sigma$ $\mu-\sigma$ μ $\mu+\sigma$ $\mu+2\sigma$

2. Experimental study: Purpose: to determine of a treatment has an effect on the population.

Large Population

1. Sample (measure)

2. Calculate some statistics that summarize the data.

3. Treatment

4. Sample (measurement)

5. Calculate some statistics that summarize the data.

6. Compare statistics from treatment to the "expected" values (pre-treatment)

34%   34%

13.5%   13.5%

0.15%   2.35%   2.35%   0.15%

$\mu - 2\sigma$ $\mu - \sigma$ μ $\mu + \sigma$ $\mu + 2\sigma$
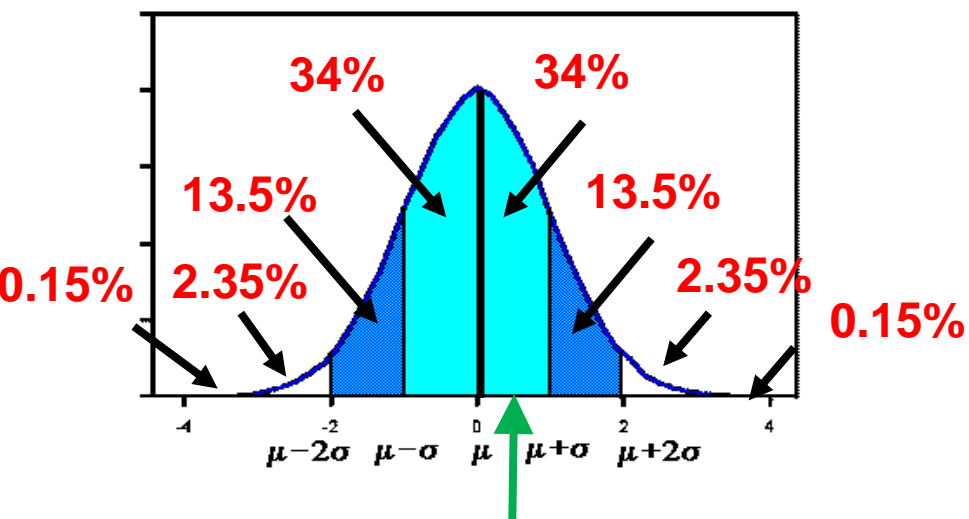
3. <u>Observational study</u>: Purpose: to see if there is a correlation between parameters of the population.

Large Population

1. Sample (measure 'A')

2. Sample (measure 'B')

3. Compare 'A' to 'B' by graphing
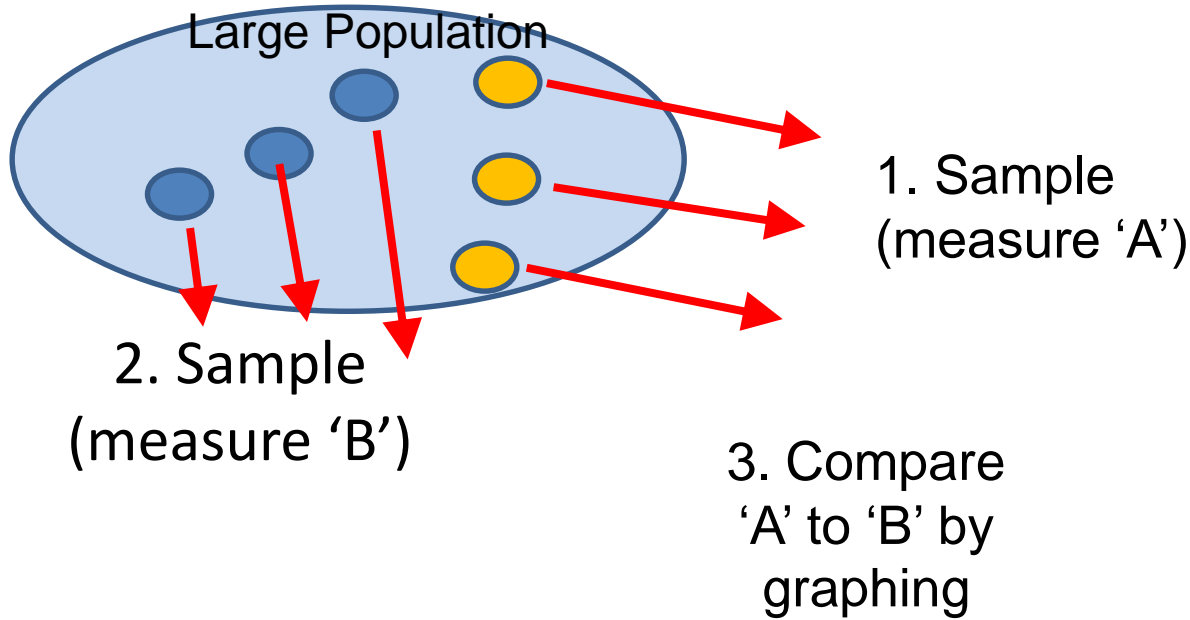
4. Is there correlation?

$\dfrac{\text{\# problems}}{\text{HW assignment}}$	Ave Test score
20	80
30	85
40	74
50	77

$\dfrac{\text{logs}}{\text{hr}}$	room temp
0	65
1	70
2	74
3	78
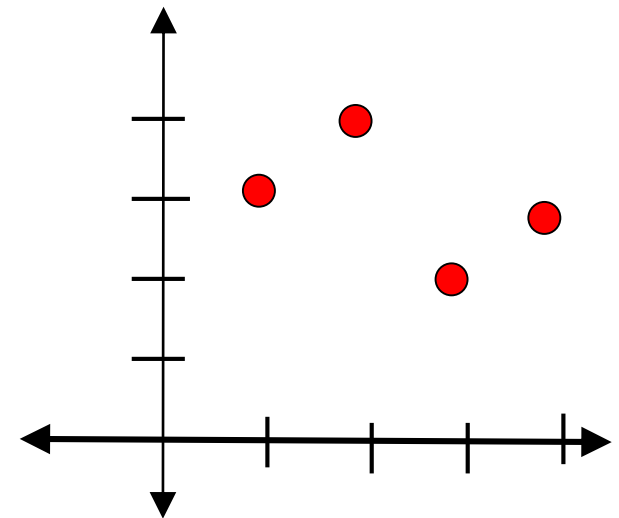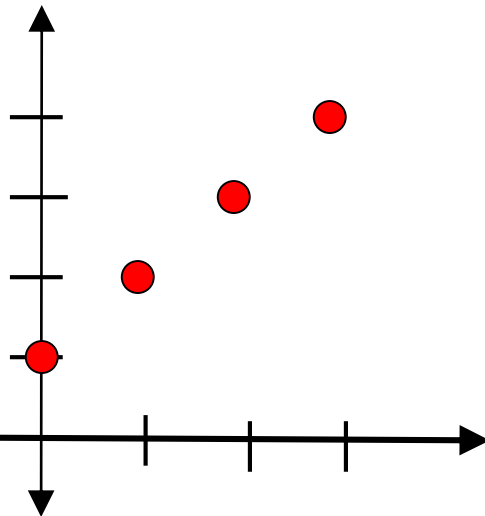
If we want to study the <u>variation in height of individuals</u> in a certain population what statistics would we want from that population?

Mean   Standard deviation

If the population is very large, it is unpractical to measure every member of the population. What do we do?

<u>Take a sample</u> from the population and obtain statistics from the sample. We than assume that the sample statistics reflect the statistics of the underlying population.

What can we do to maximize the probability that the statistics of the sample are representative of the statistic of the population?

The sample must be completely randomized so that every individual has the same chance of being selected.

Types of Samples:

1. Self-selected sample.   completely randomized ?

   Members of the sample group volunteer to participate in the sample.

2. Convenience sample.   completely randomized ?

   Easy-to-reach members of the population are used.

3. Systematic sample.   completely randomized ?

   A rule is used to select individuals.

4. Random sample.   completely randomized ?

   Each member of the population has an equal chance of being selected.

In statistics, **sampling bias** is a bias in which a sample is collected in such a way that some members of the intended population are less likely to be included than others. If this is not accounted for, results can be erroneously attributed to the phenomenon under study rather than to the method of sampling.

Sampling bias merely represents a mathematical property, no matter if it is deliberate or either unconscious or due to imperfections in the instruments used for observation.

Are the following examples of sample bias? If so, would this indicate that the underlying population is <u>healthier</u> or <u>less</u> healthy than it actually is?

1. Sampling workers at a factory to measure the health of the general population.

sample is likely <u>healthier</u> than the general population.

2. Sampling current companies to measure the health of the economy?.

sample is likely <u>healthier</u> than the general population.

3. Using questions by using words like "sometimes" and "often" in your survey.

Requires individual interpretation.

Are the following examples of sample bias? If so, would the sample be <u>healthier</u> or <u>less</u> healthy than the underlying population?

4. Taking temperatures of people in a hospital waiting room.

sample is likely <u>less healthy</u> than the general population.

5. Measuring cholesterol in participants of P90X exercise class?

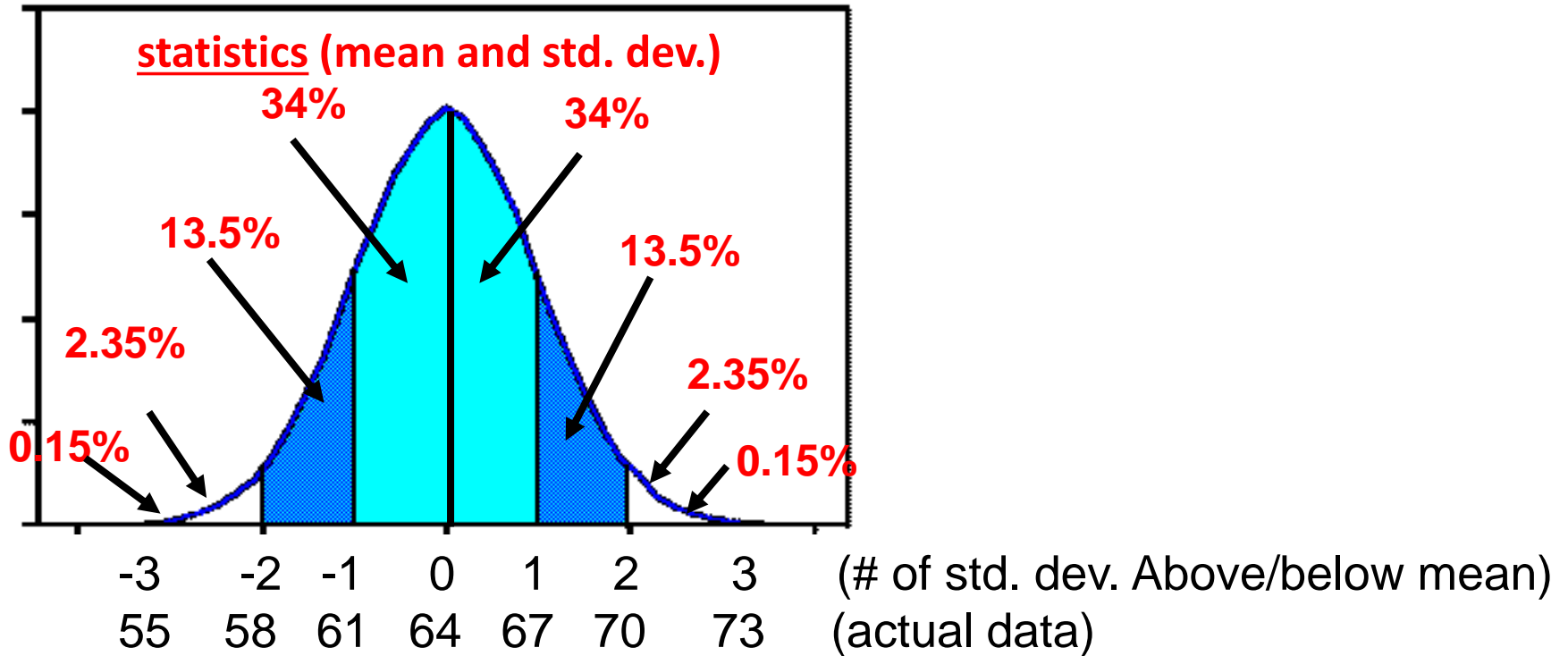sample is likely <u>healthier</u> than the general population.

6. Measuring IQ scores on campus at Harvard University.

Sample is likelier <u>higher</u> than the general population.

Types of Samples and the potential for <u>bias</u>:

| Sample Type	Potential for bias?
Self-selected	often
convenience	often
Systematic	sometimes
random	<u>Unbiased!</u>

If our sample is randomly selected, then the <u>variability</u> in the sample is <u>due to randomness of the underlying population rather than some bias</u> in the sampling method.

<u>statistics</u> (mean and std. dev.)

-3	-2	-1	0	1	2	3	(# of std. dev. Above/below mean)
55	58	61	64	67	70	73	(actual data)

99.7% Confidence Interval: if we repeated the same sampling method to select different data sets, and re-computed the +/- 3 SDEV for each of these different data sets, we would expect the mean of the underlying population to fall within +/- 3 SDEV 99.7% of the time.
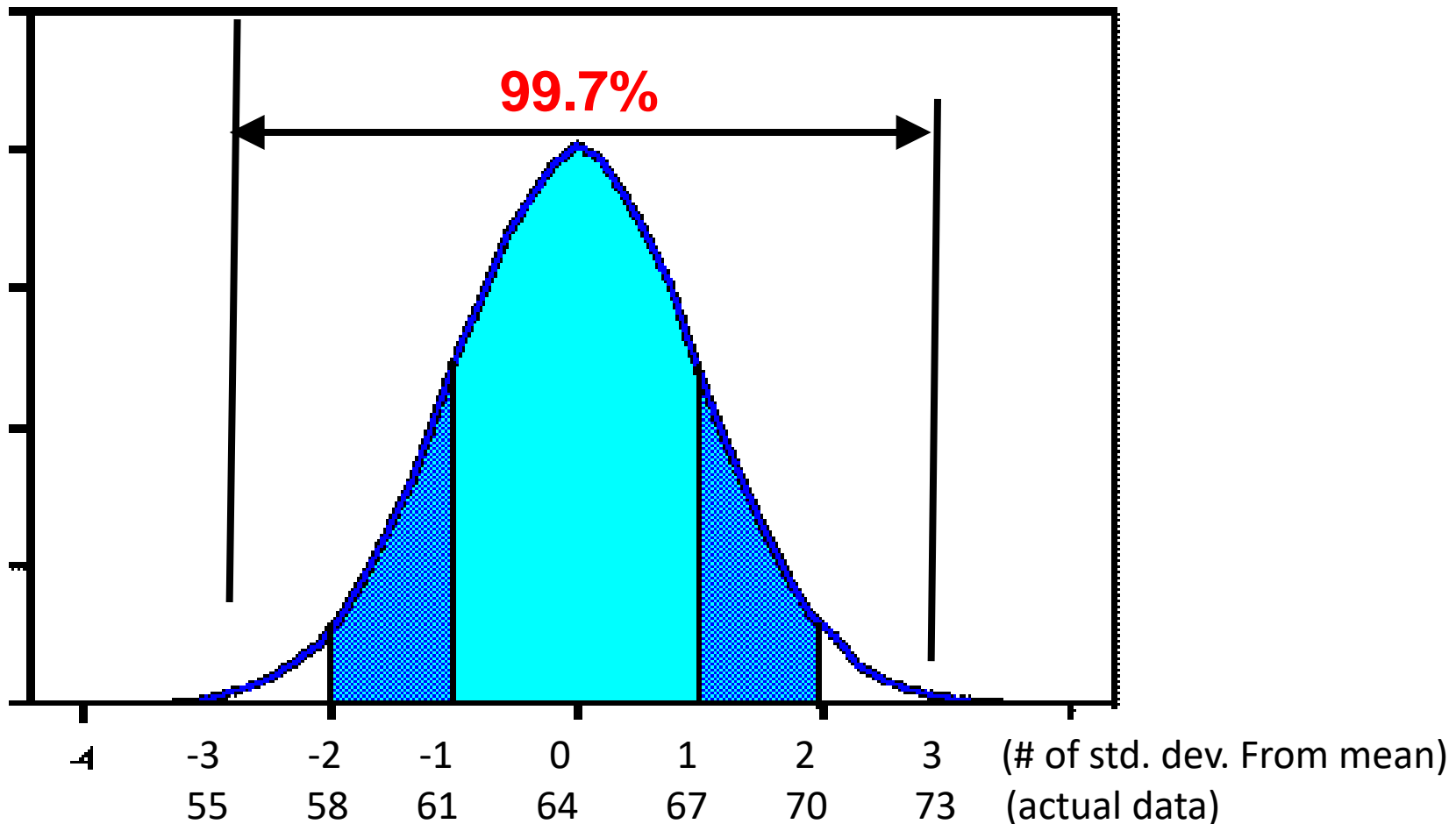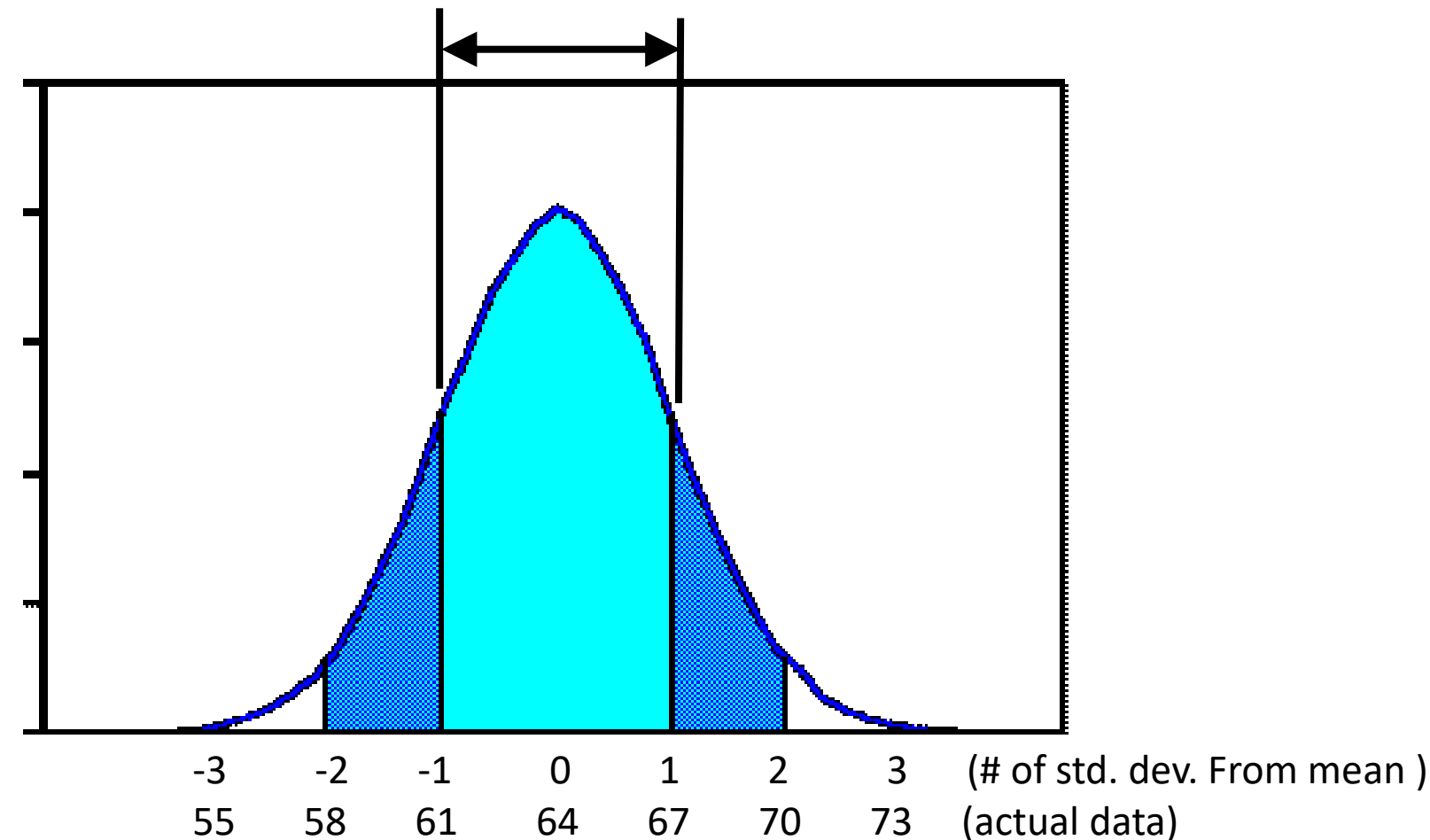
95% Confidence Interval: if we repeated the same sampling method to select different data sets, and re-computed the +/- 2 SDEV for each of these different data sets, we would expect the mean of the underlying population to fall within +/- 2 SDEV 95% of the time.

| | -3 | -2 | -1 | 0 | 1 | 2 | 3 | (# of std. dev. From mean) |
| | 55 | 58 | 61 | 64 | 67 | 70 | 73 | (actual data) |
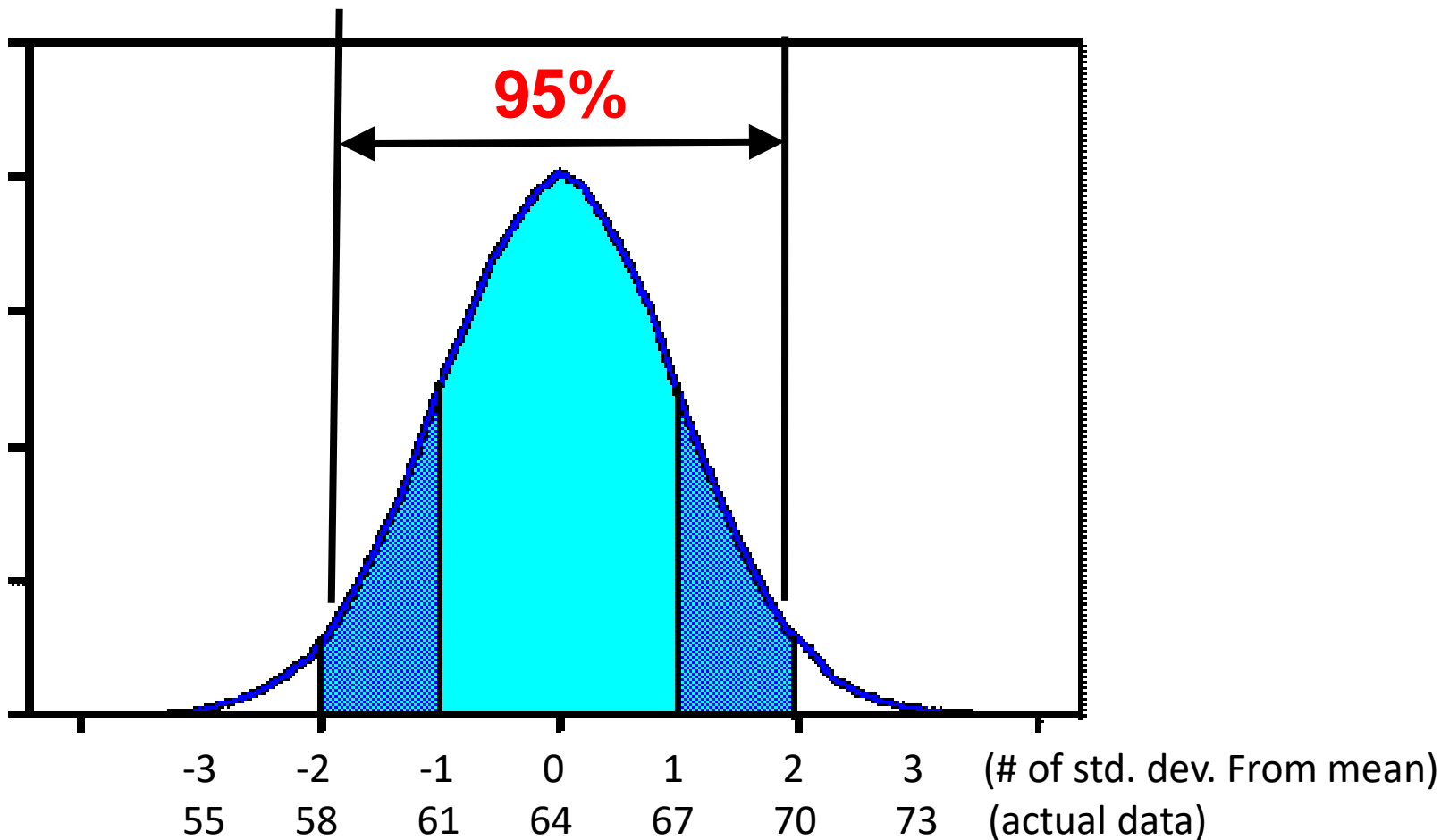
68% Confidence Interval: if we repeated the same sampling method to select different data sets, and re-computed the +/- 1 SDEV for each of these different data sets, we would expect the mean of the underlying population to fall within +/- 1 SDEV 68% of the time.

-3	-2	-1	0	1	2	3	(# of std. dev. From mean)
55	58	61	64	67	70	73	(actual data)

95% Confidence Interval: the colored region.

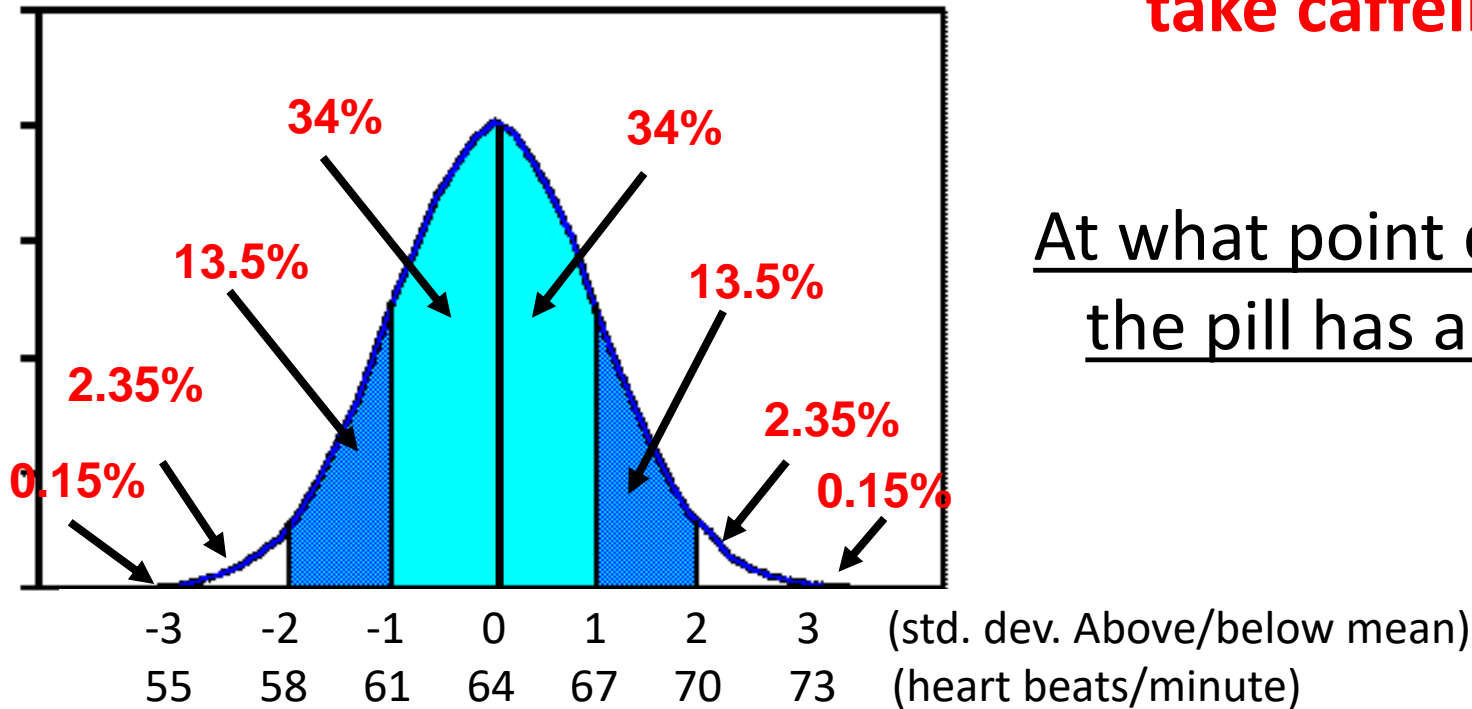statistics (mean and std. dev.)
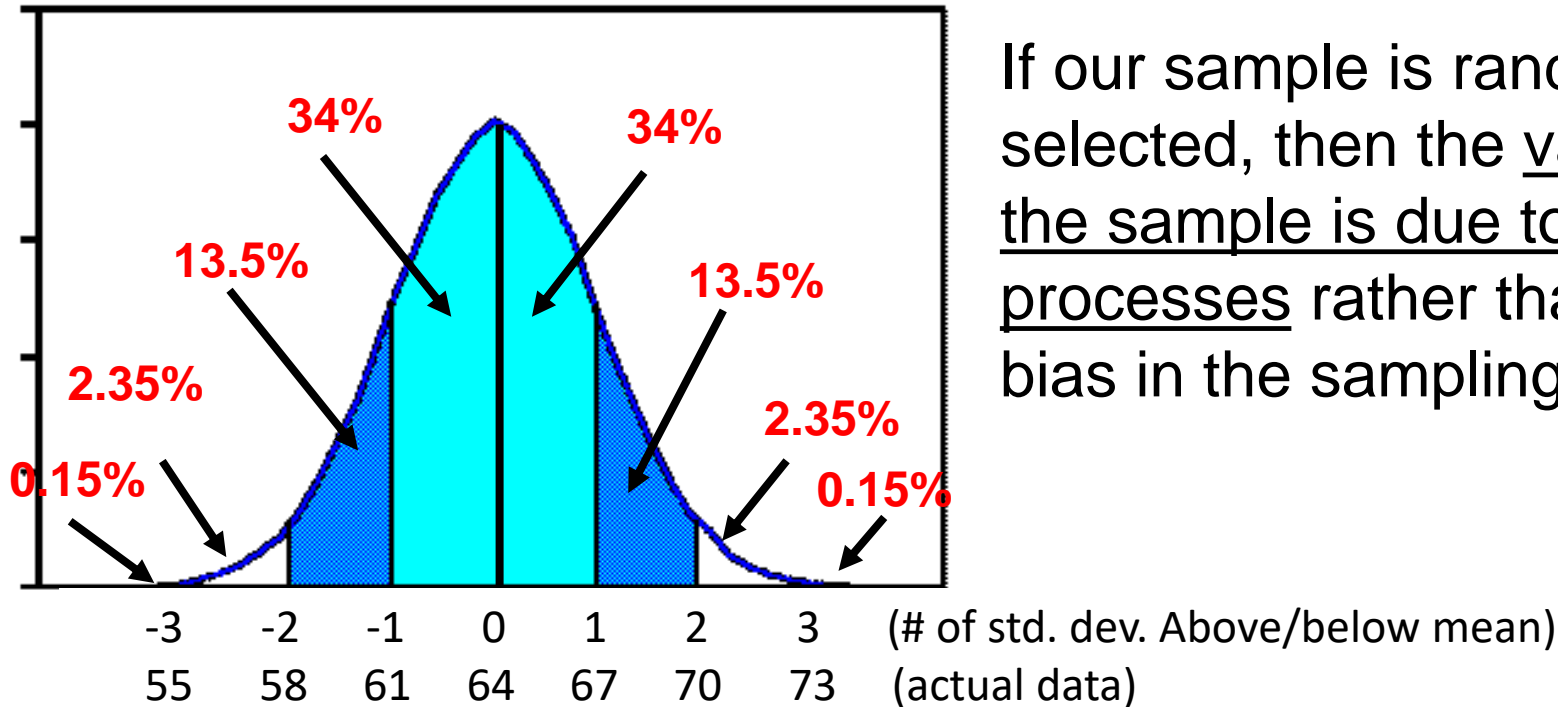
If our sample is randomly selected, then the variability in the sample is due to random processes rather than some bias in the sampling method.

The "confidence interval" combines an estimate of the interval in which the population mean falls, and a probability of the repeatability of where the mean would fall given the same sample procedure.
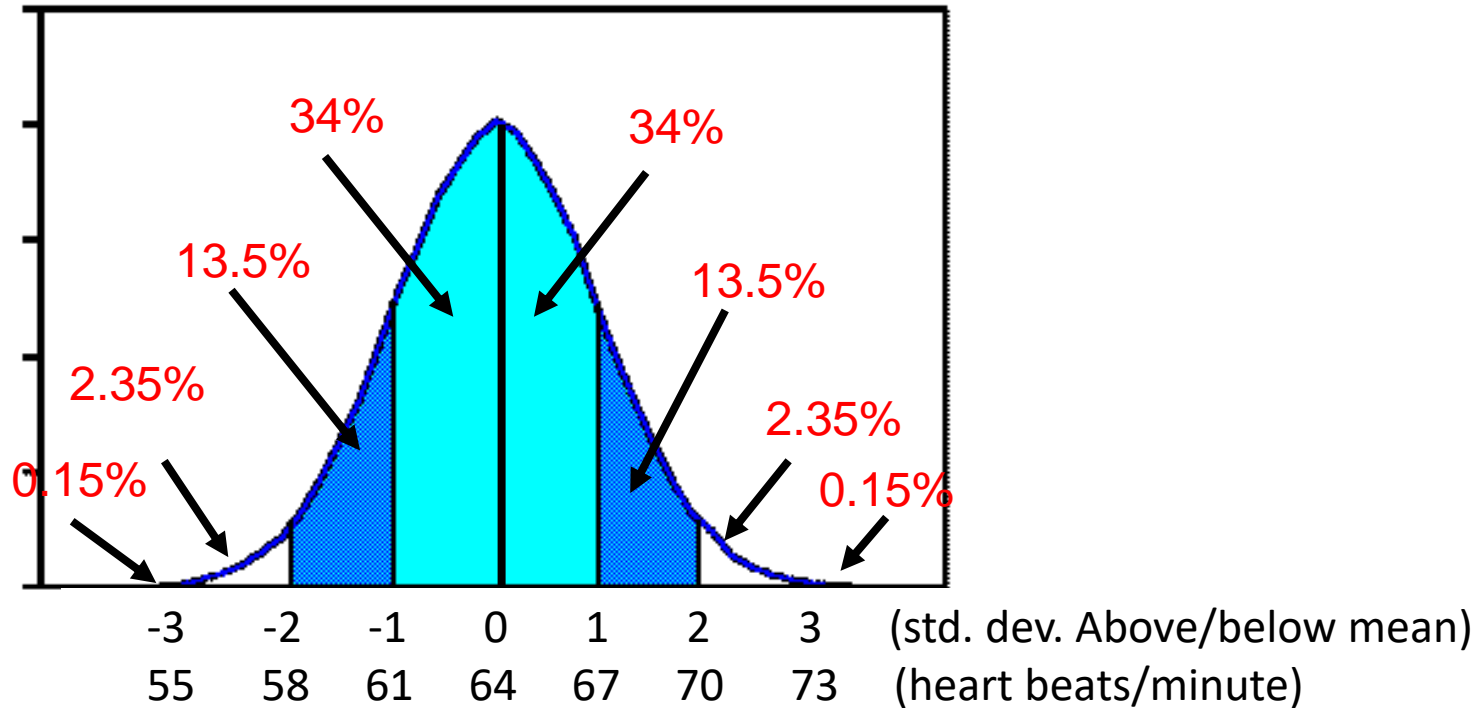
95% Confidence Interval: the colored region.

At what point do you say the pill has an effect?

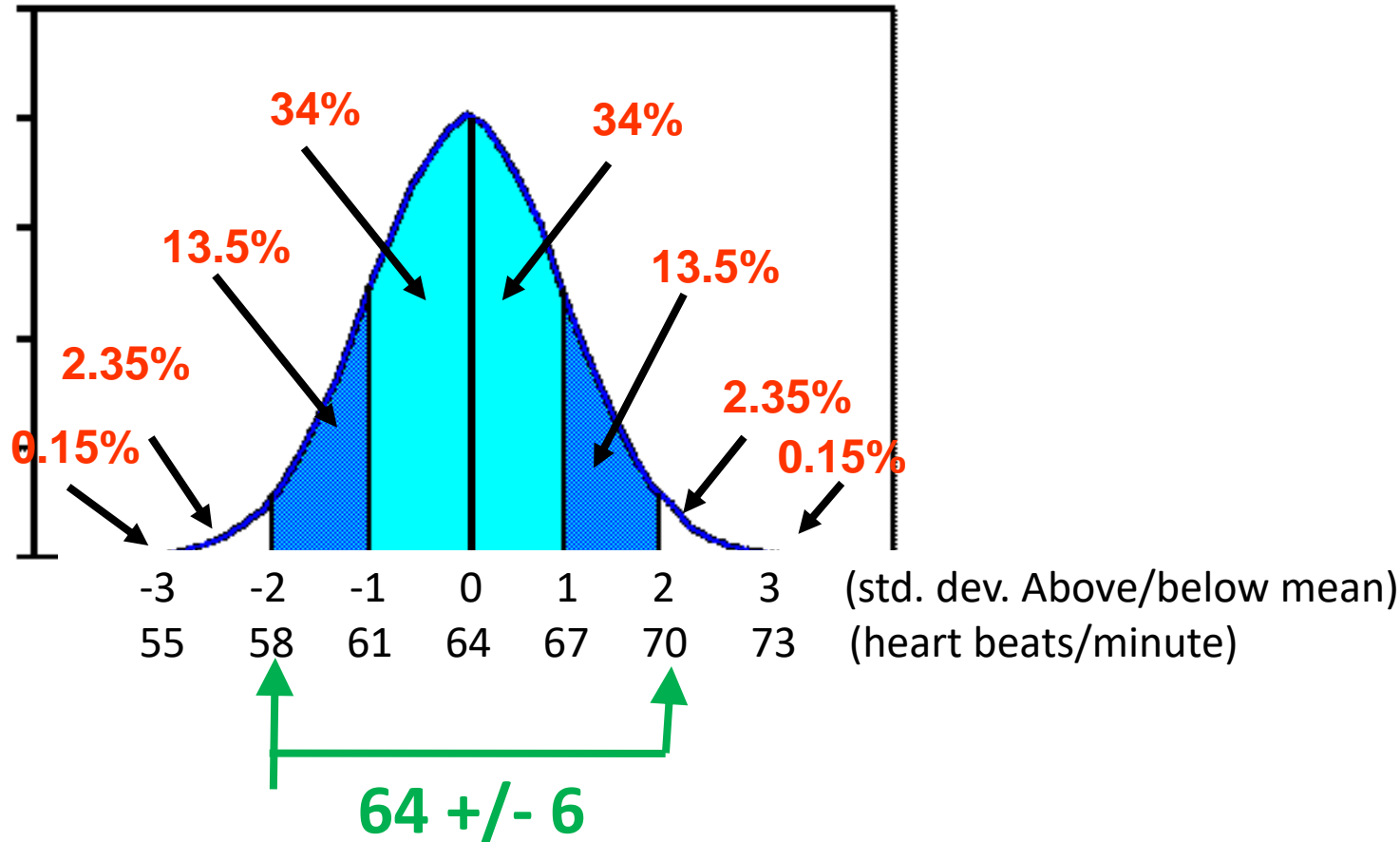statistics (mean and std. dev.) **prior to** taking the pill

34% 34%

13.5% 13.5%

2.35% 2.35%

0.15% 0.15%

| -3 | -2 | -1 | 0 | 1 | 2 | 3 | (std. dev. Above/below mean) |
| 55 | 58 | 61 | 64 | 67 | 70 | 73 | (heart beats/minute) |

Mean heart rate after pill

1

95% Confidence Interval:

What is the 95% confidence interval for the data below?

statistics (mean and std. dev.) **prior to** taking the pill

64 +/- 6

95% confidence interval: 58 to 70 BPM

You want to conduct an experiment to determine if adding fertilizer results in more flowers blooming on petunias.

2. How would you set up the experiment so that you could test this factor only?

  a. Randomly select 'x' number of Petunias seeds.

  b. Number each pot (from 1 to 'x').

  c. Put numbers 1 to 'x' into a hat and select 'x'/2 numbers. This is the control group. The other plants are the treatment group.

d. Place all plants <u>randomly</u> (x spots, randomly selected from a "hat") in a green house and provide the same soil, water, sunlight, etc.

  e. Control group gets same amount of fertilizer.

You want to conduct an experiment to determine if adding fertilizer results in more flowers blooming on petunias.

3. Why can we say the statistics from this experiment represent that of the underlying population?

Random selection of seeds for control and treatment, along with random positioning inside the green house ensures the sampling method does not introduce bias into the experiment.

The random variation within the population is not being over-represented in either the control or treatment samples. Therefore the sample results should represent the underlying population.

If we repeated the same sampling method to select different seeds and re-computed the +/- 2 SDEV for the parameter of interest (mean number of blooms), we would expect the mean of the underlying population to fall within this interval 95% of the time.