SM3-A HANDOUT 7-8 (Base 'e': Continuous Growth and Decay)

A rental property has a market value of \$150,000. The owner rents out the property for \$1100 per month.

What percentage of the market value of the house does the owner charge for rent each month?

$$\frac{part}{whole} = ? \quad \frac{1100}{150000} = 0.0073 \quad = 0.73\% / month$$

What percentage of the market value of the house does the owner charge for rent for the whole year?

$$\frac{part}{whole} = ? \frac{1100 * 12}{150000} = \frac{13200}{150000} = \frac{8.8\%}{year}$$

Rent

A landlord ends up charging a total of \$18,000 for a tenant to rent a \$200,000 house for a year (ouch).

What percentage of the market value of the house does the owner charge for rent for the year?

$$\frac{part}{whole} = ? \frac{18000}{200000} = 0.09 = \frac{9\%}{yr}$$

What percentage of the market value of the house does the owner charge for rent for a month?

Can you rent money?
"Rent" $ ightarrow$ To pay for the possession and use of something.
Give an example of how money is "rented".
1
2
For each case, who is the "landlord" and who is the "tenant"?
1. savings account \rightarrow are the landlord.
2. Borrow money→is the landlord.
The interest rate for borrowing money is always given as an annual interest rate, but "rent" can be paid at the <u>end of the year</u> , the <u>end of every 6 months</u> , the <u>end of each month, etc</u> .

You deposit \$100 money into an account that pays 3.5% interest per year. The "rent" is "paid" yearly. How much money will be in the account at the end of the 1st year?

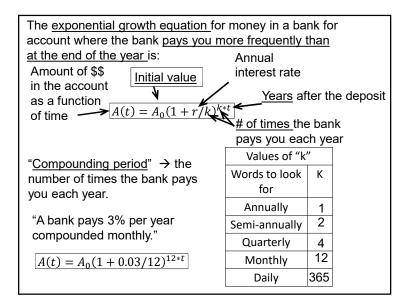
How much will be in the account after the 2nd year?

$$A(t) = A_0 (1+r)^t$$

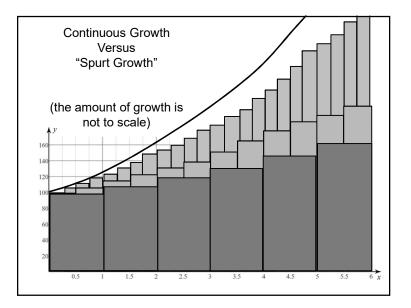
 $A(t) = A_0 (1+r)^t$

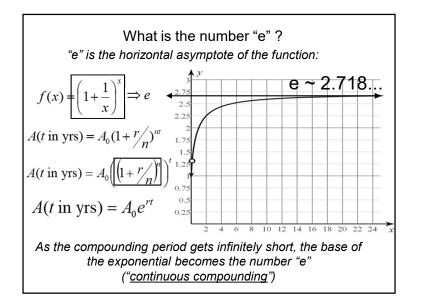
You deposit \$100 money into an account that pays 3.5% interest per year. But the "rent" is paid "monthly." What is the interest rate that is paid each month?

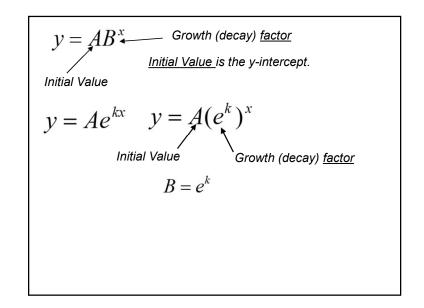
 $\frac{3.5\%}{year} * \frac{1 \text{ year}}{12 \text{ months}} = \frac{0.29\%}{month} = \frac{0.0029}{month}$ How much money will be in the account after 5 months? $A(t) = A_0(1+r)^t$ $A(5) = 100(1+0.0029)^5 \quad \text{Time uses units of <u>months}</u>$ A(5 months) = \$101.45How much money will be in the account after 7 years? $A(7 \text{ years}) = 100(1+0.0029)^{12(7)} \quad \text{Time uses units of <u>years.</u>}$ $A(7 \text{ years}) = 100(1+0.0029)^{12(7)} \quad \text{Time uses units of years.}$ $A(7 \text{ years}) = 100(1+0.0029)^{12(7)} \quad \text{Time uses units of years.}$ $A(7 \text{ years}) = 4_0(1+r/n)^{nt}$ a(7) = \$127.54"n": number of times "rent" is paid per year

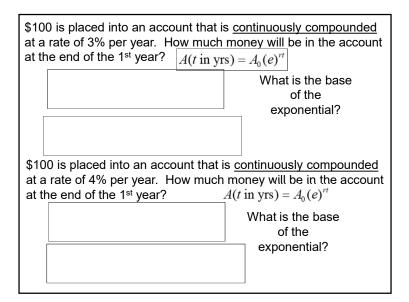


<u>Compound interest</u>: the interest (rent) that is paid at the end of period of time. $A(t \text{ in yrs}) = A_0(1 + \frac{r}{n})^{nt}$ Compounded annually: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{n})^{1*t}$ Compounded semi-annually: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{2})^{2*t}$ Compounded quarterly: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{4})^{4*t}$ Compounded monthly: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{4})^{4*t}$ Compounded weekly: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{4})^{4*t}$ Compounded daily: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{52})^{52*t}$ Compounded daily: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{52})^{52*t}$ Compounded hourly: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{365})^{365*t}$ Compounded hourly: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{8760})^{8760*t}$ Compounded minutely: "n" = ? $A(t \text{ in yrs}) = A_0(1 + \frac{r}{525600})^{525600*t}$









$$y = 4^x = e^{1.386x}$$
look at the pattern of
the exponents of 'e' $y = 1.1^x = e^{0.095x}$ book at the pattern of
the exponents of 'e' $y = 1.01^x = e^{0.010x}$ $y = e^{kx}$ $y = 1^x = e^{(0)x}$ Growth: $y = 0.85^x = e^{-0.163x}$ Decay: $y = 0.25^x = e^{-1.386x}$ Decay: $y = B^x$ Growth: B > 1Decay: 0 < B < 1