

SM2 THEOREMS 7-2 (Distance and Triangle Congruence)

The Pythagorean Theorem:

IF the triangle is a right triangle,

THEN the lengths of the sides are related by: $a^2 + b^2 = c^2$

Theorem is a statement that has been proven to be true.

Theorems are usually written in

“IF hypothesis , THEN conclusion ” format.

Theorem: IF (it is a) dog, THEN (it) barks

Converse of

the Theorem: IF it barks , THEN it is a dog



If the hypothesis is true then we know the conclusion is true.

We exchange the hypothesis and conclusion to get a converse.

The converse of Pythagorean theorem is also the true (but this doesn't work for all theorems).

Pythagorean Theorem

IF the relationship between the side of a triangle make the following statement true, $a^2 + b^2 = c^2$

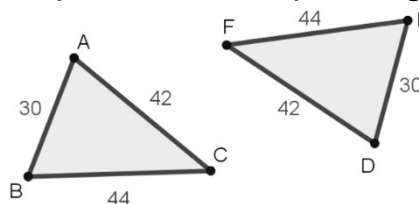
THEN the it is a right triangle.

SM2 THEOREMS 7-2 (Continued)

Side-Side-Side (SSS) Congruency Axiom: if all three pairs of corresponding sides of a triangle are congruent, then the triangles are congruent

$$\overline{AB} \cong \overline{DE}, \overline{BC} \cong \overline{EF}, \text{ and } \overline{CA} \cong \overline{FD}$$

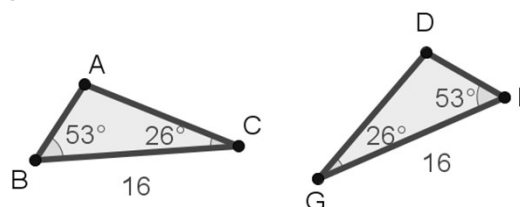
Therefore, $\triangle ABC \cong \triangle DEF$ by **SSS**



Angle-Side-Angle (ASA) Congruency Axiom: if two angles and their included side are congruent, then the two triangles are congruent.

$$\angle ABC \cong \angle DEG; \overline{BC} \cong \overline{EG}; \angle BCA \cong \angle EGD$$

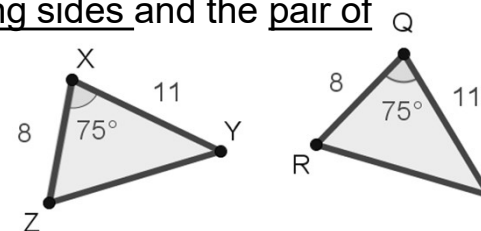
Therefore, $\triangle ABC \cong \triangle DEG$ by **ASA**



Side-Angle-Side (SAS) Congruency Axiom: if two pairs of corresponding sides and the pair of included angles are congruent, then the triangles are congruent.

$$\overline{XZ} \cong \overline{QR}, \angle ZXY \cong \angle RQF, \text{ and } \overline{XY} \cong \overline{QF}$$

Therefore, $\triangle XYZ \cong \triangle QFR$ by **SAS**



Angle-Angle-Side (AAS) Congruency Axiom: If two pairs of corresponding angles are congruent and one pair of corresponding sides are congruent (which are NOT the included side), then the two triangles are congruent.

$$\angle ZXY \cong \angle EFD, \angle XYZ \cong \angle FDE, \overline{XZ} \cong \overline{FE}$$

Therefore, $\triangle XYZ \cong \triangle FDE$ by **AAS**

