

Math-2

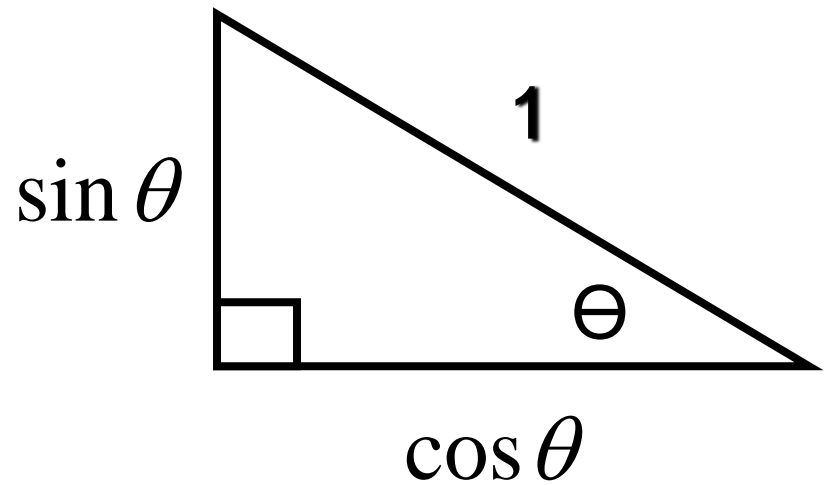
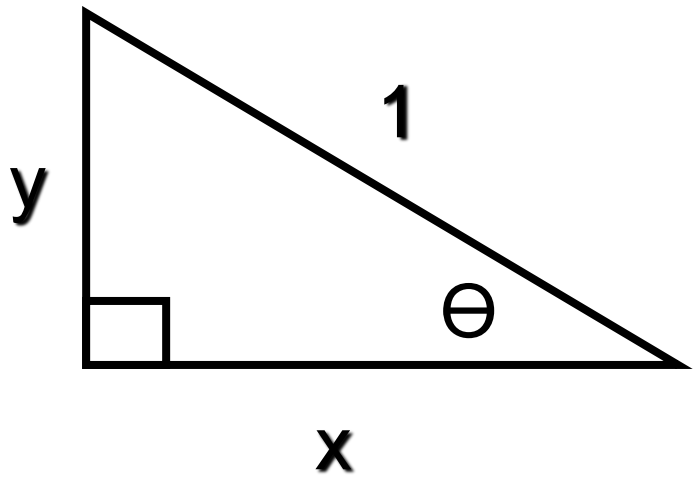
8-6

Pythagorean Identity,

Tangent lines and Secant lines of circles,

Non-central/inscribed angles of Circles,

Dilations and Rotations on the XY Plane



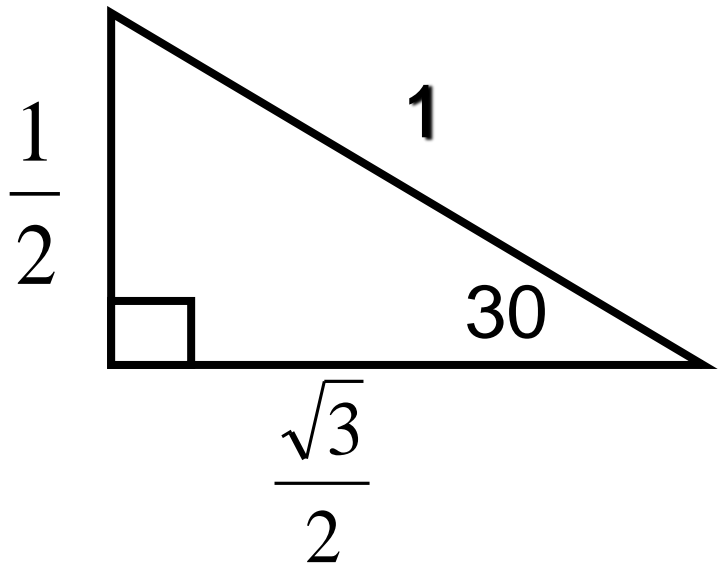
$$\sin \theta = y$$

$$\cos \theta = x$$

Back substitute to the triangle.

Write Pythagorean relationship for the triangle.

$$\sin^2 \theta + \cos^2 \theta = 1$$



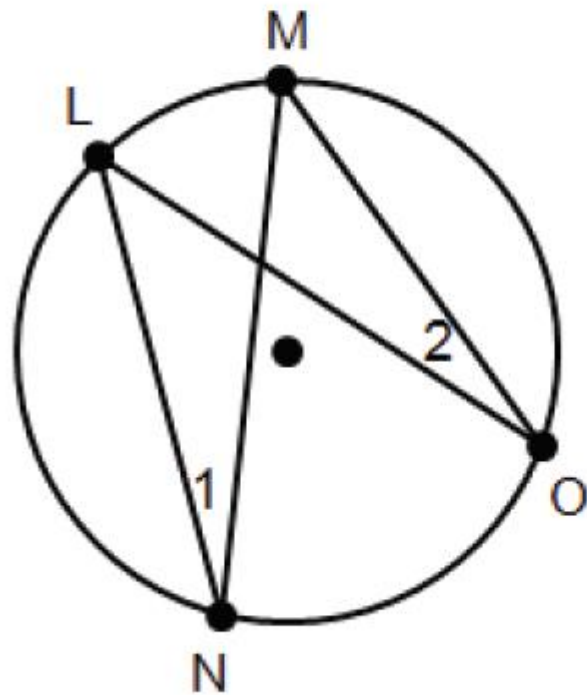
$$\sin 30 = \frac{1}{2} \quad \cos 30 = \frac{\sqrt{3}}{2}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

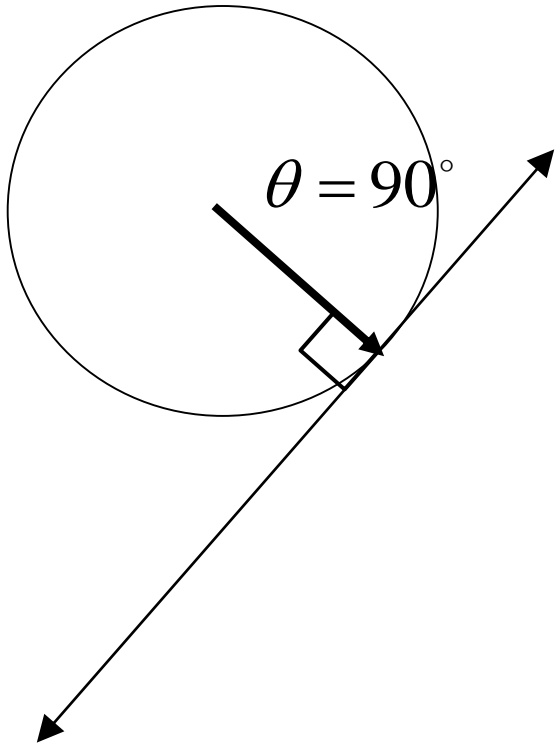
$$\left(\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2 = 1$$

$$\frac{1}{4} + \frac{3}{4} = 1$$

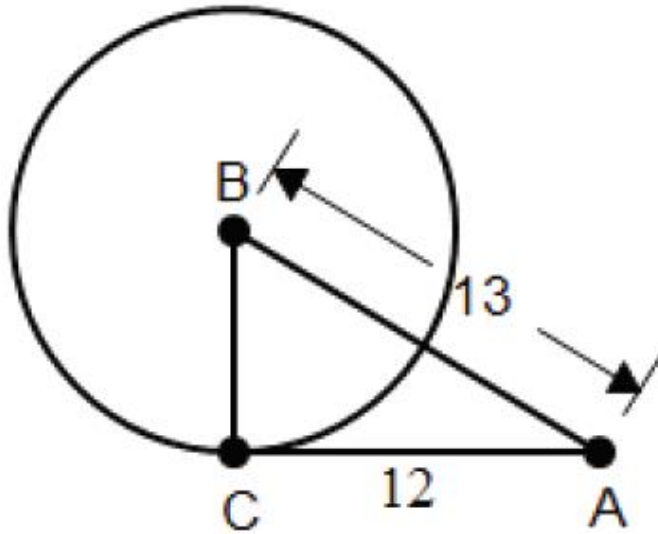
Find the measure of angles 1 and 2 if
 $m\angle 1 = 2x - 13$ and $m\angle 2 = x$.



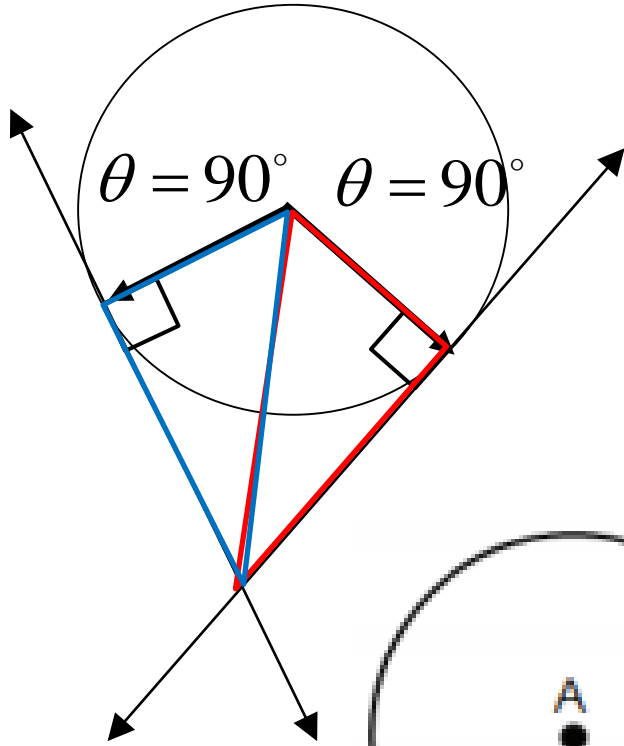
If a tangent to a circle intersects at the endpoint of a radius, then the angle of intersection is 90° .



Segment AC is tangent to Circle B at point C. Find BC



If a tangent to a circle intersects at the endpoint of a radius, then the angle of intersection is 90° .

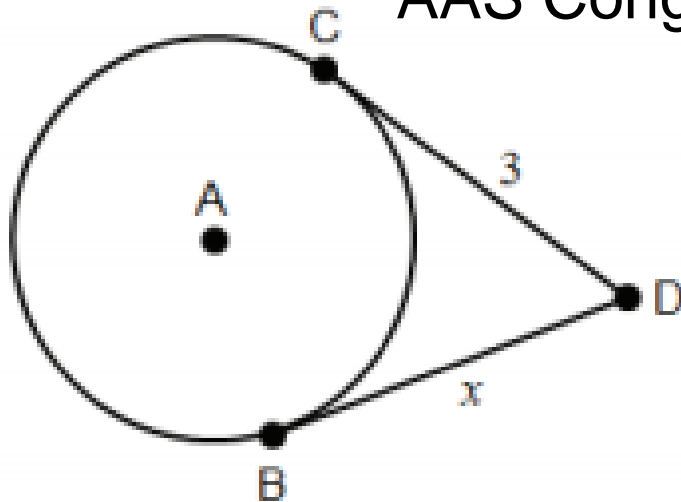


Are the two triangles congruent? If so, what congruence theorem can you use to prove congruence?

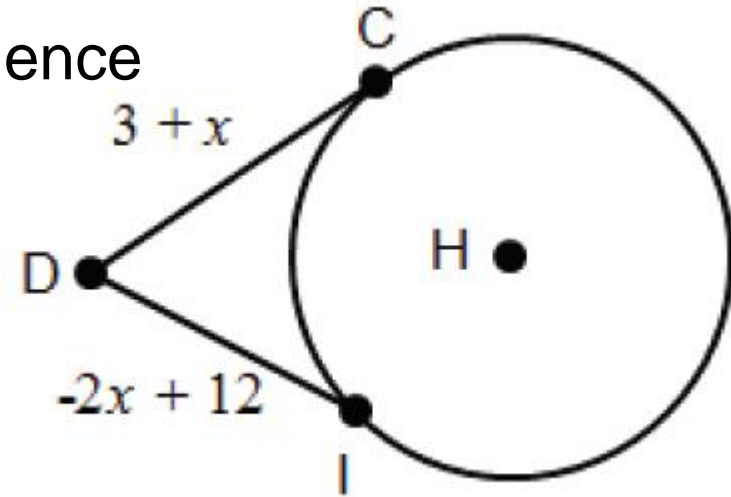
Shared side is congruent

Pair of legs are radii \rightarrow congruent

AAS Congruence



$$x = 3$$

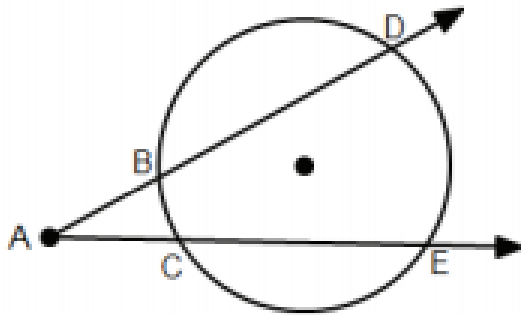


$$-2x + 12 = 3 + x$$

$$x = 3$$

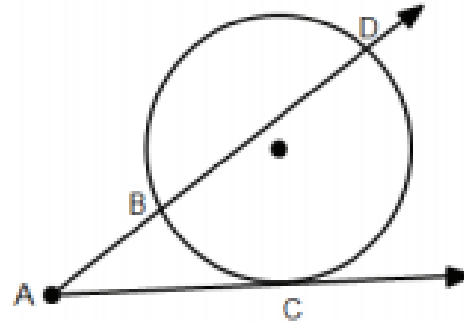
If two secant lines cut a circle then the angle of intersection is one half of the difference between the intercepted arcs.

Two Secants



$$m\angle A = \frac{1}{2}(mDE - mBC)$$

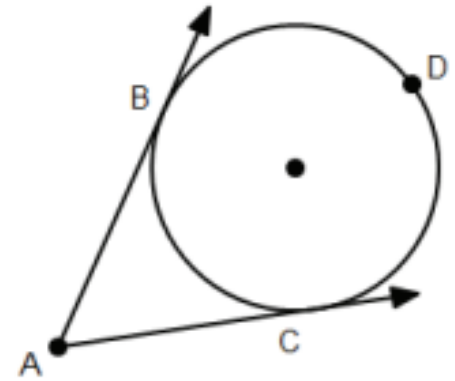
Secant and Tangent



$$m\angle A = \frac{1}{2}(mDC - mBC)$$

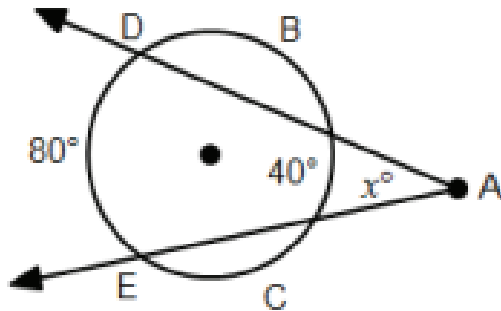
Same for a secant and a tangent line.

Two Tangents



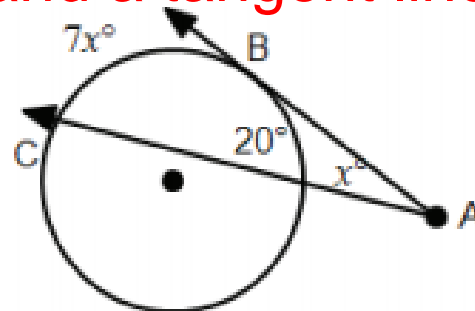
$$m\angle A = \frac{1}{2}(mCDB - mBC)$$

Same for two tangent lines.



$$x = 0.5(80 - 40)$$

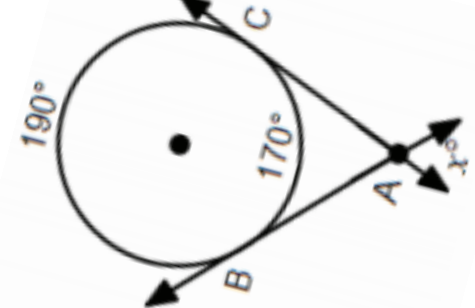
$$x = 20$$



$$x = 0.5(7x - 20)$$

$$2x = 7x - 20$$

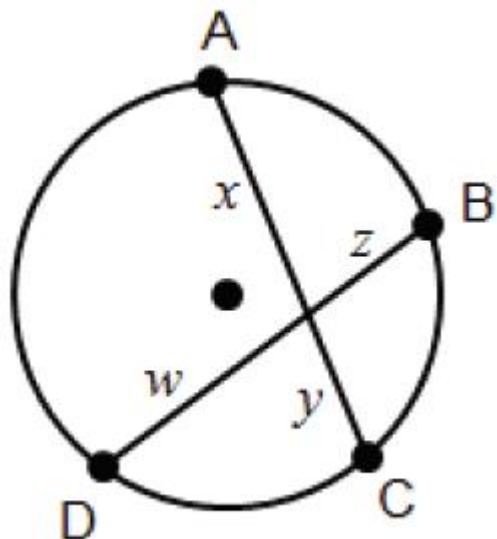
$$x = 4$$



$$x = 0.5(190 - 170)$$

$$x = 10$$

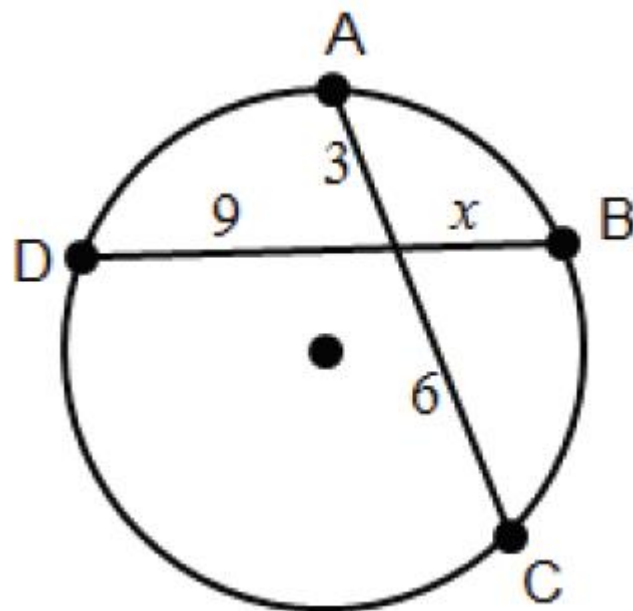
If two chords intersect inside a circle, then the product of the lengths of the segments of one chord is equal to the product of the lengths of the segments of the other chord.



$$xy = wz$$

$$9x = 3(6)$$

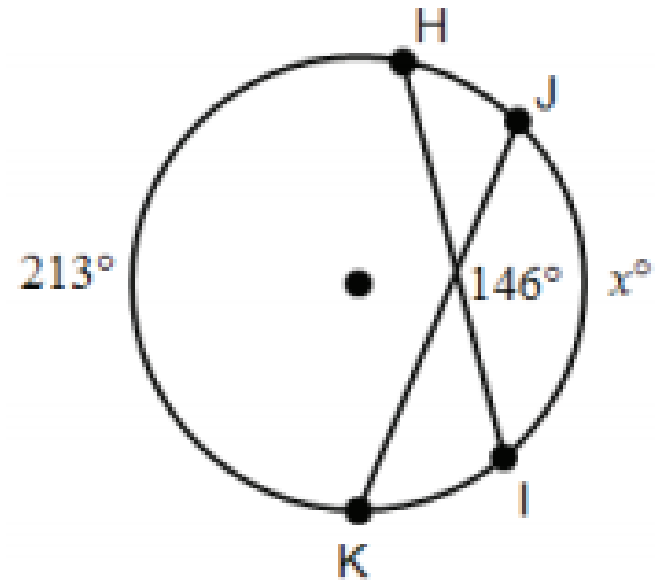
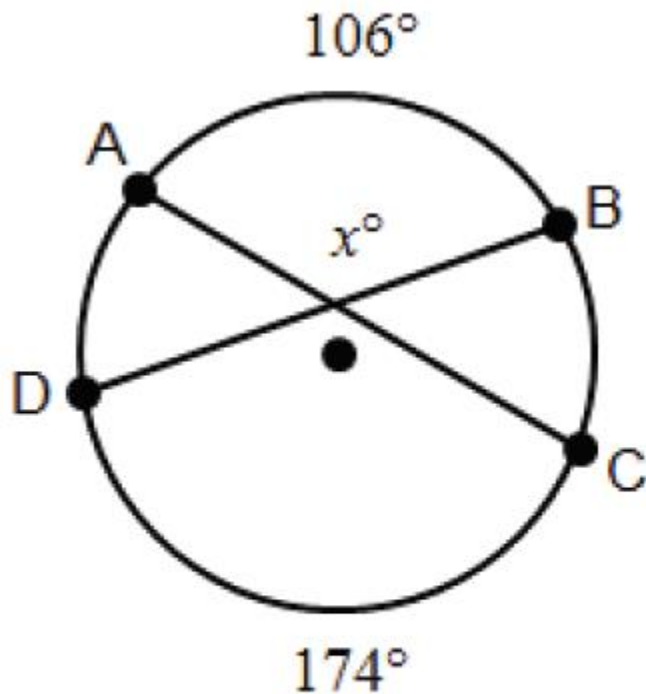
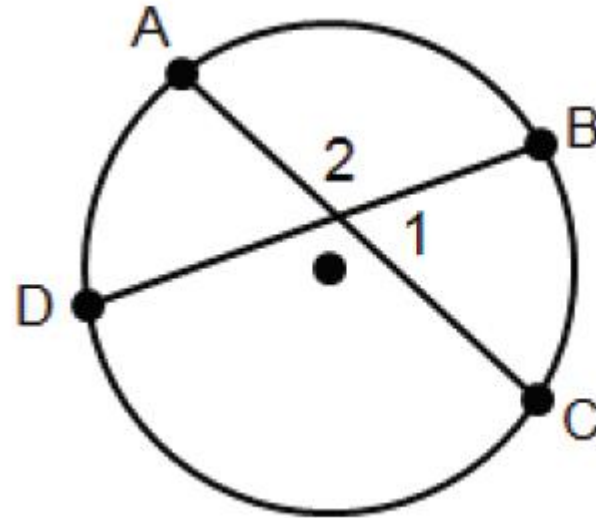
$$x = 2$$



If 2 chords intersect inside of a circle then the measure of the angle is the average of the two intercepted arcs.

$$m\angle 2 = \frac{1}{2}(m\overline{CD} + m\overline{AB})$$

$$m\angle 1 = \frac{1}{2}(m\overline{BC} + m\overline{AD})$$



Do the segments that connect the points form a parallelogram?

$$F(2,1), G(1,4), H(5,4), \text{ and } J(6,1)$$

→ YES

The Hard Way

1. Find all the segment lengths (opposite sides of parallelograms are congruent).

$$GF = \sqrt{(2-1)^2 + (1-4)^2} = \sqrt{1^2 + (-3)^2} = \sqrt{1+9} = \sqrt{10}$$

$$HJ = \sqrt{(5-6)^2 + (4-1)^2} = \sqrt{(-1)^2 + 3^2} = \sqrt{1+9} = \sqrt{10}$$

$$FJ = \sqrt{(6-2)^2 + (1-1)^2} = \sqrt{4^2 + 0^2} = \sqrt{16} = 4$$

$$GH = \sqrt{(5-1)^2 + (4-4)^2} = \sqrt{4^2 + 0^2} = \sqrt{16} = 4$$

YES

2. Find all the slopes between the points (opposite sides are parallel).

$$m_{GF} = \frac{1-4}{2-1} = \frac{-3}{1} = -3$$

$$m_{HJ} = \frac{4-1}{5-6} = \frac{3}{-1} = -3$$

$$m_{FJ} = \frac{1-1}{6-2} = \frac{0}{4} = 0$$

$$m_{GH} = \frac{4-4}{5-1} = \frac{0}{4} = 0$$

YES

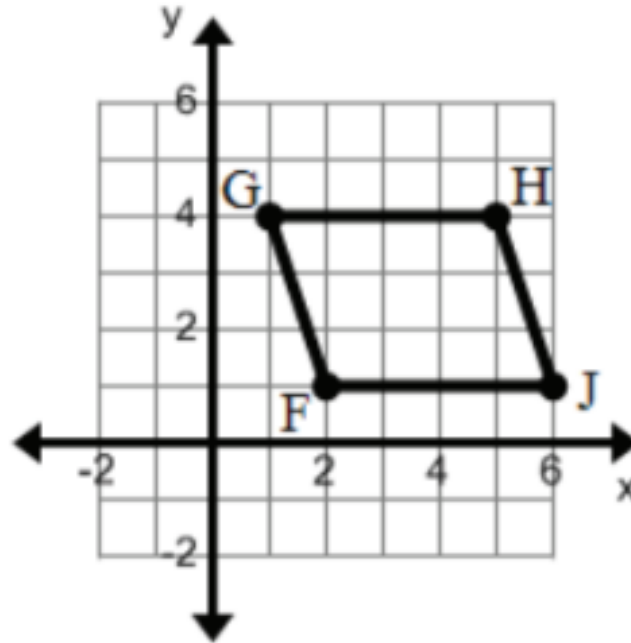
Do the segments that connect the points form a parallelogram?

$F(2,1)$, $G(1,4)$, $H(5,4)$, and $J(6,1)$

→ YES

The Easy Way

1. Graph the points



2. Are opposite sides congruent?

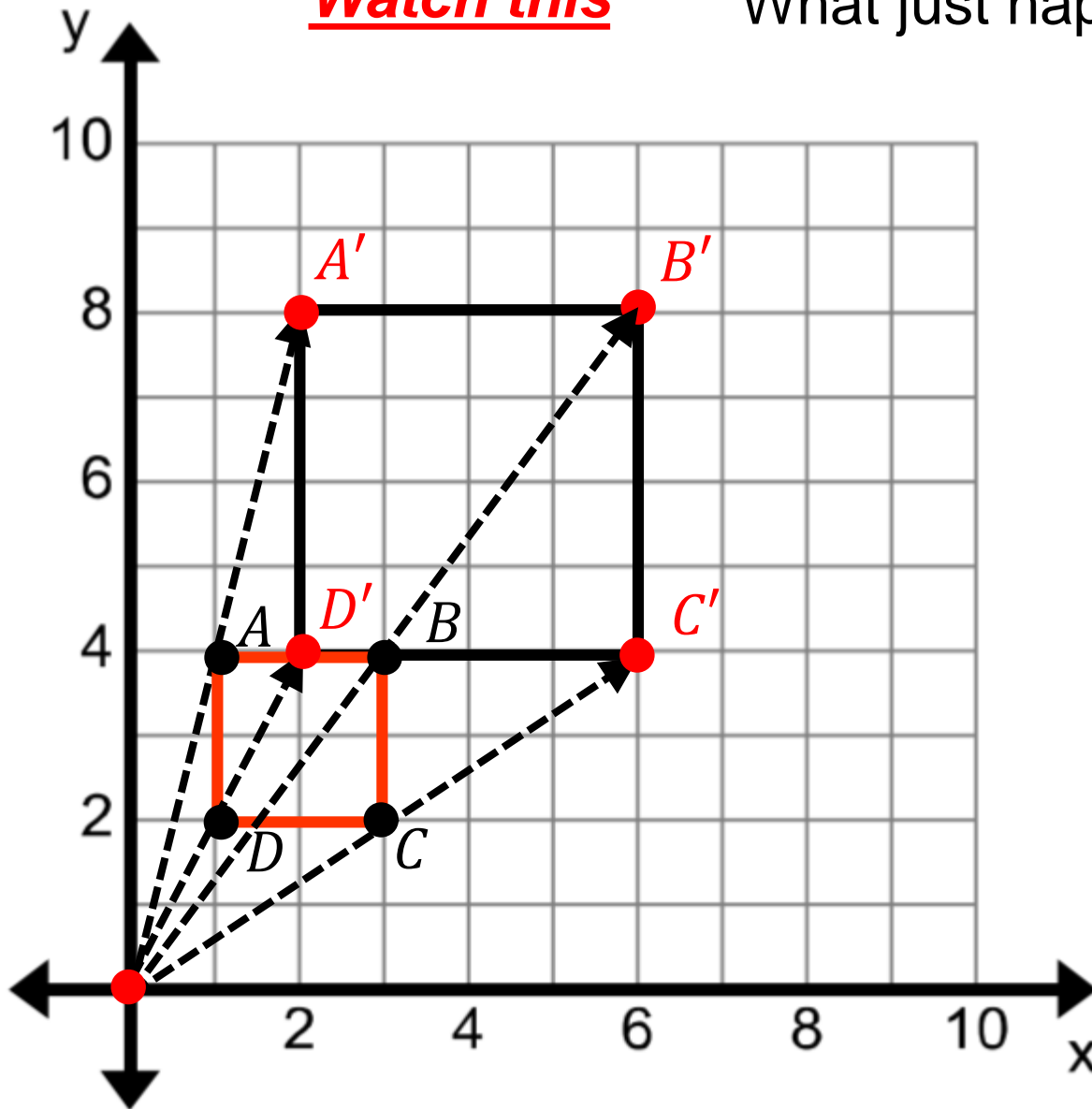
YES

3. Are opposite sides parallel?

YES

Watch this

What just happened?

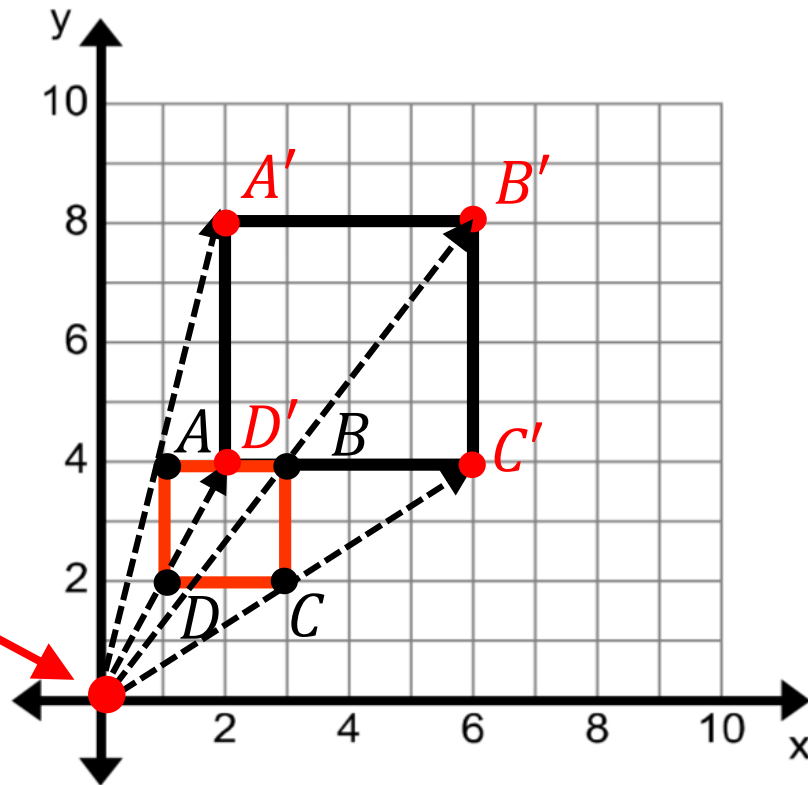


Dilation: a transformation that results in the same shape but a different size. It uses a center of dilation and a scale factor to create the proportional figure.

Center of Dilation: a fixed point in the x-y plane about which all points of the figure are expanded or contracted.

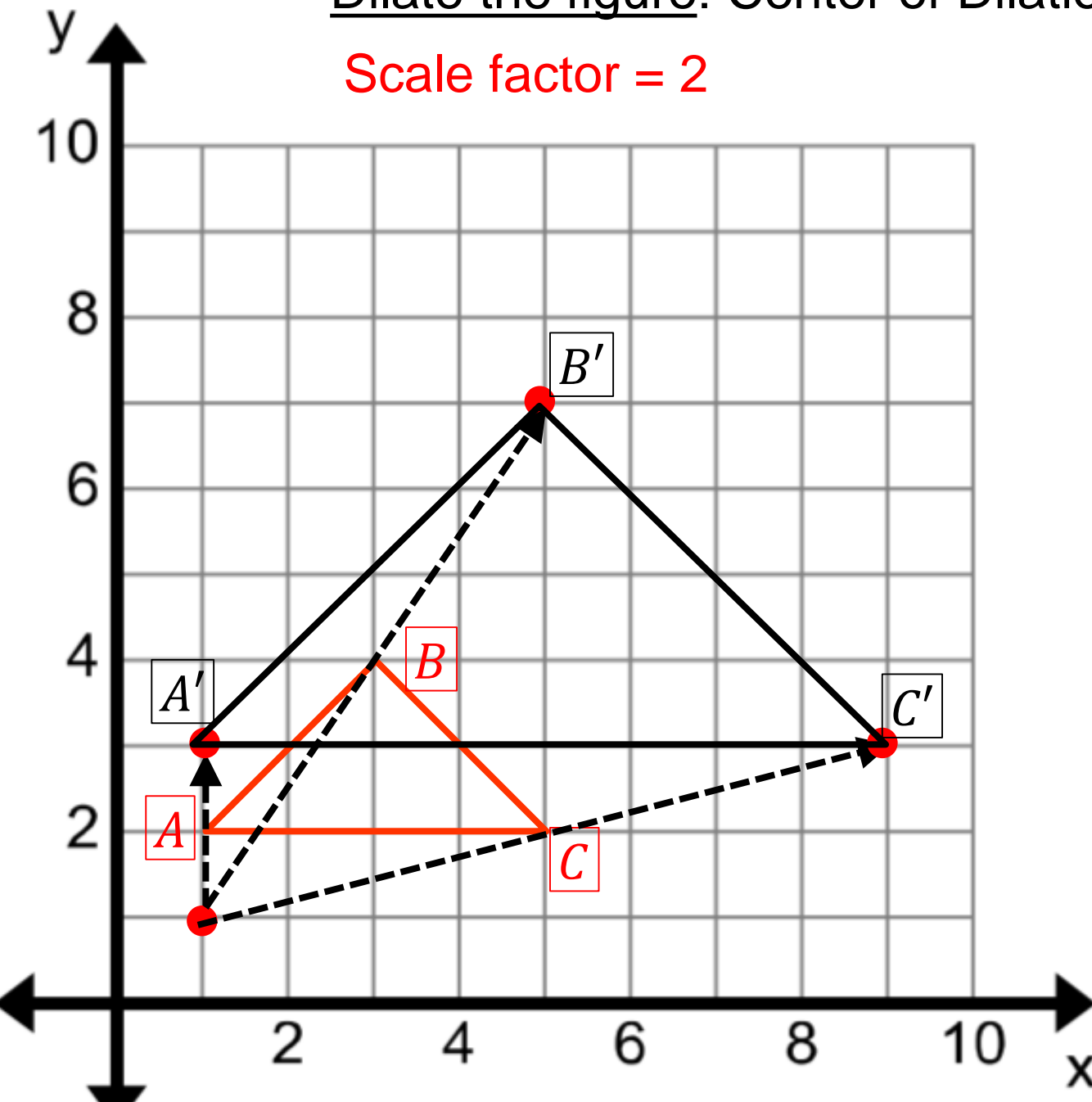
Center of Dilation: (0, 0)

$$\text{Scale factor} = \frac{A'B'}{AB} = \frac{4}{2}$$



Dilate the figure: Center of Dilation: (1, 1).

Scale factor = 2



Rotate the shape 90° in the clockwise direction.

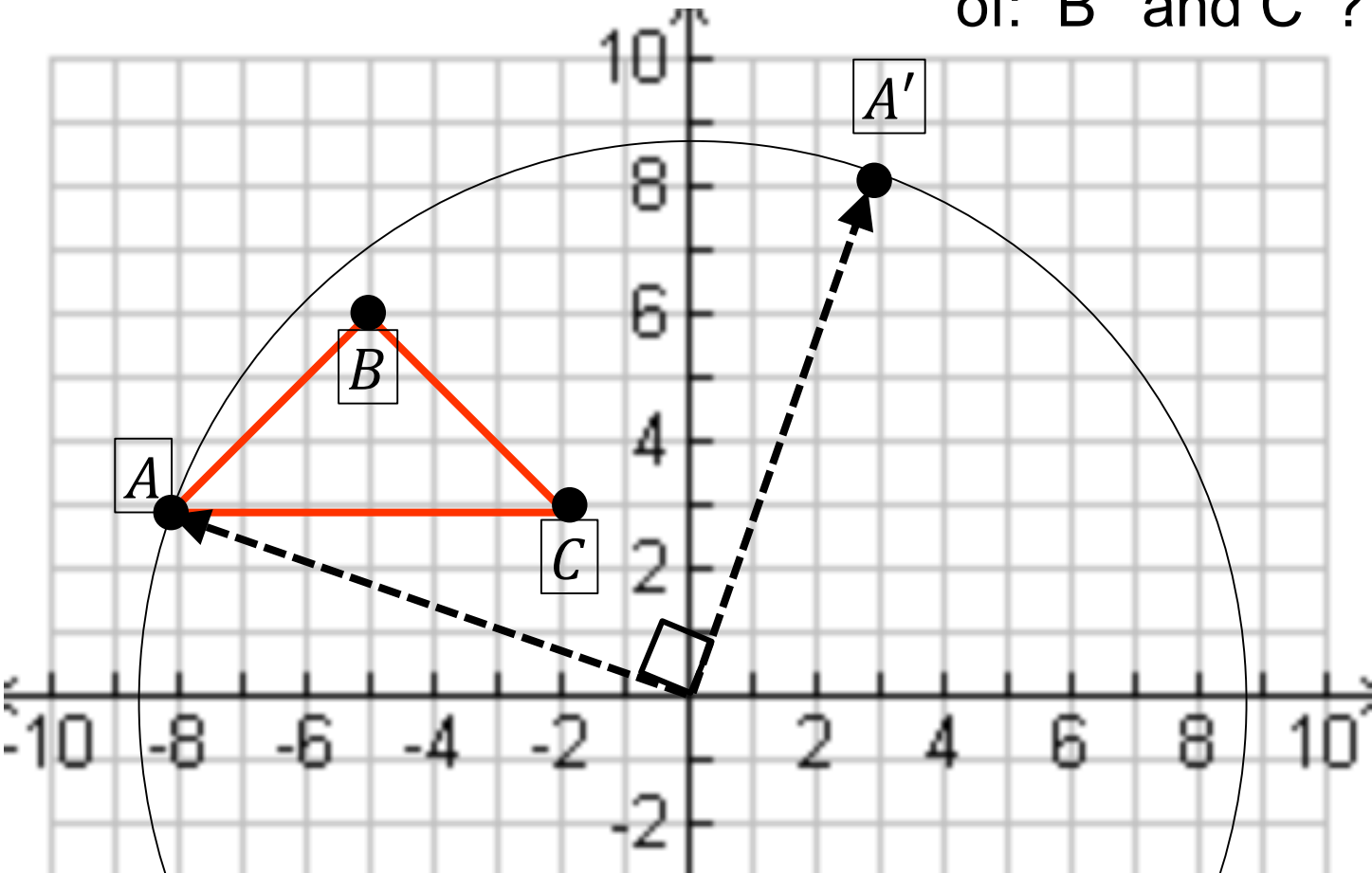
Compare the two x-y pairs. $A: (-8, 3)$ $A': (3, 8)$

1) Moves the point to the adjacent quadrant of the x-y plane \rightarrow +/- of points may (or may not change).

2) x-y values are exchanged.

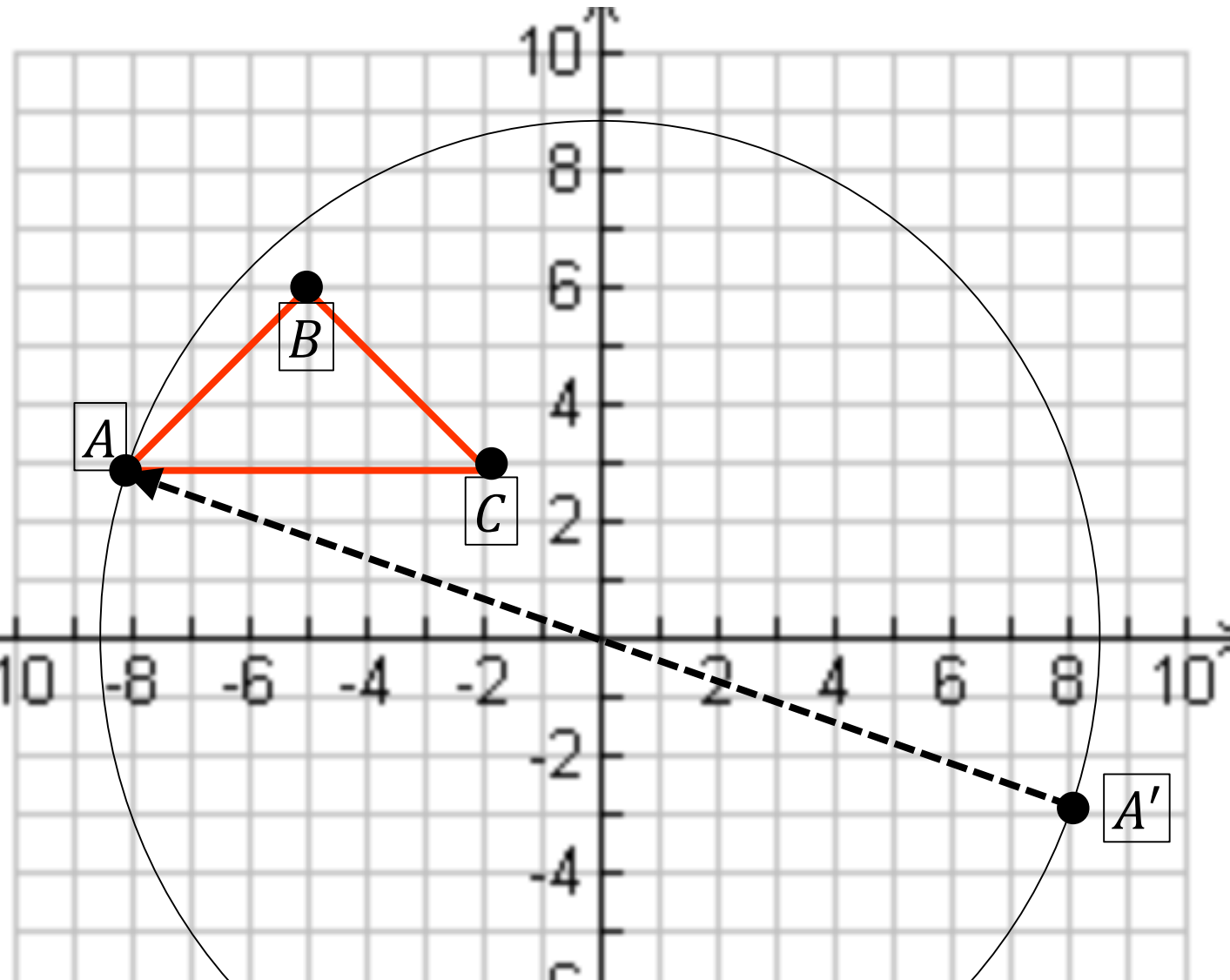
What are the coordinates of: B' and C' ? $B': (5, 5)$

$C': (3, 2)$



Rotate the shape 180° in the clockwise direction.

A: $(-8, 3)$ A': $(8, -3)$ Moves the point to the opposite quadrant of the x-y plane \rightarrow +/- of points change.



What are the coordinates of: B' and C' ?

B': $(5, -6)$

C': $(2, -3)$