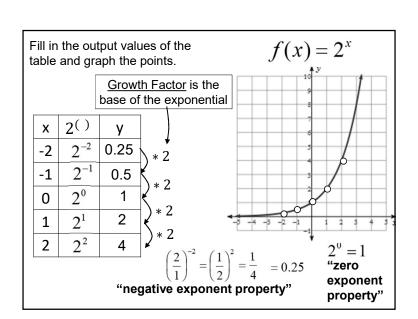
Math-2 Lesson 9-3

Exponential Function



The "Parent" Exponential Function

$$y = b_{\text{base}}^{x}$$

 $\gamma=2^{\chi}$ (base 2 exponential function)

 $v=3^{\chi}$ (base 3 exponential function)

$$y = \left(\frac{1}{2}\right)^{x}$$
 (base 1/2 exponential function)

The base MUST BE positive and CANNOT equal 1.

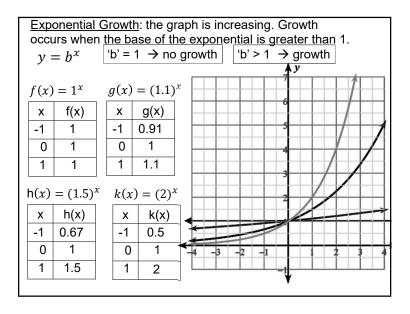
$$b=(0,1)\cup(1,\infty)$$

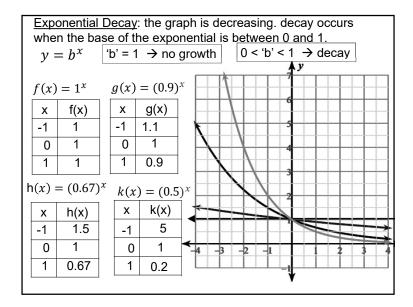
Exponential Function $f(x) = 2^x$

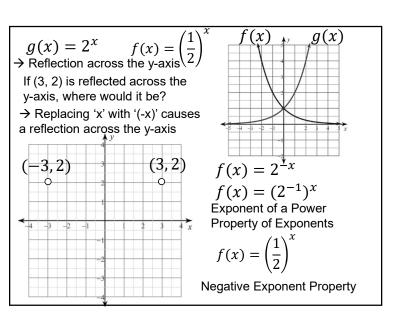
Will the 'y' value ever reach zero (on the left end of the graph)? As the denominator gets bigger and bigger, the decimal version of the fraction gets smaller and smaller.

Х	2()	У	'y' gets closer and closer to zero but <u>never reaches zero.</u>					
-1	2 ⁽⁻¹⁾	$\frac{1}{2}$	$f(-1) = \frac{1}{2}$					
-2	2 ⁽⁻²⁾	$^{1}/_{4}$	$f(-2) = \frac{1}{4}$					
-3	2 ⁽⁻³⁾	1/8	$f(-3) = \frac{1}{8}$					
-4	2 ⁽⁻⁴⁾	1/16	$f(-4) = \frac{1}{16}$					
-5	2 ⁽⁻⁵⁾	1/32	$f(-5) = \frac{1}{32} \downarrow$					
	-		•					

Horizontal Asymptote: a horizontal line the graph approaches but never reaches. y = 0 Domain = ? $x = (-\infty, \infty)$ range = ? $y = (0, \infty)$ y-intercept = ? $f(0) = y \ intercept$ $f(0) = 2^0 = 1$



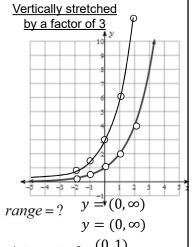




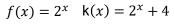
$f(x) = 2^x \qquad g(x) = 3(2)^x$						
х	,	2()	f(x)	g(x)		
-2	2	2^{-2}	0.25	0.75		
-1	L	2^{-1}	0.5	1.5		
0)	2°	1	3		
1		2 ¹	2	6		
2		2^2	4	12		
Horizontal $y = 0$						

 $Domain = ? \quad x = (-\infty, \infty)$ $x = (-\infty, \infty)$

asymptote: y = 0



(0,1)y-intercept = ? (0,3)

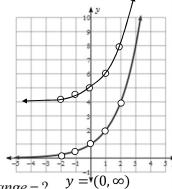


Х	2()	f(x)	k(x)
			<u> </u>
-2	2^{-2}	0.25	4.25
-1	2^{-1}	0.5	4.5
0	2°	1	5
1	21	2	6
2	2 ²	4	8

Horizontal y = 0asymptote: y = 4

 $Domain = ? \quad x = (-\infty, \infty)$ $x = (-\infty, \infty)$

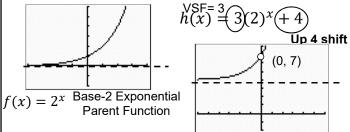


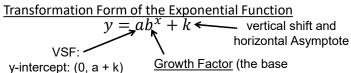


range = ? $y = (4, \infty)$

(0, 1)y-intercept = ? (0,5)

Transformations of the Exponential Function





of the exponential)

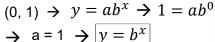
$$h(0) = 3(2)^0 + 4$$
$$h(0) = 7$$

Summary

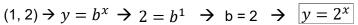
- $g(x) = ab^x + k$ 1) Start with
- 2) Find the value of 'k' (horizontal asymptote).

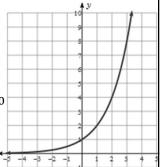
$$g(x) = ab^x + k \quad \Rightarrow \quad y = ab^x$$

3) Substitute the y-intercept



4) Substitute a "nice" x-y pair from the graph into the equation.





What is the equation of the graph?

- 1) Start with $g(x) = ab^x + k$
- 2) Find 'k'

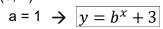
Horizontal asymptote: y = 3

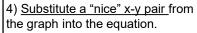
$$k = 3$$

$$k = 3 \qquad y = ab^x + 3$$

3) Substitute the y-intercept

$$(0,4) \rightarrow 4 = ab^0 + 3$$



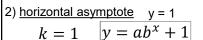


$$(1, 5) \rightarrow 5 = b^1 + 3 \rightarrow b = 2$$

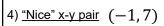
$$y = 2^x + 3$$

What is the equation of the graph?

1) Start with $g(x) = ab^x + k$



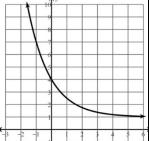
3) <u>y-intercept</u> (0,4) $4 = ab^0 + 1$ a = 3 $v = 3b^x + 1$



$$7 = 3b^{-1} + 1$$

$$6=3b^{-1}$$

$$b = 3b^{-1}$$
 $2 = \frac{1}{b}$ $b = \frac{1}{2}$ $y = 3\left(\frac{1}{2}\right)^{x} + 1$



$$y = 3\left(\frac{1}{2}\right)^x + 1$$