

SM2 HANDOUT 3-1 Equations of Lines

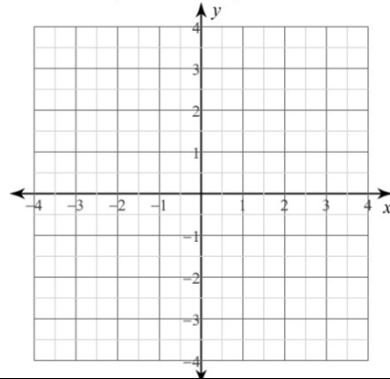
How can an equation "make" a line?

Fill in the rest
of the table

$$y = x + 1$$

Graph the x-y pairs

x	rule	y
-4	$x + 1$	
-3	$-4 + 1$	-3
-2		
-1		
0		
1		
2		
3		



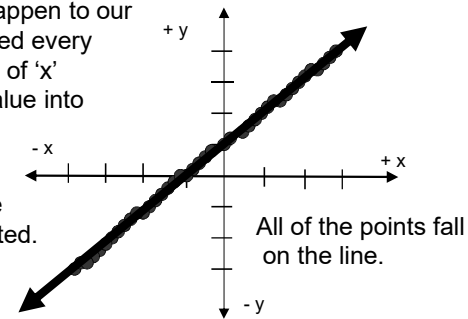
$$y = x + 1$$

So far, we've used integers and #'s halfway in between.

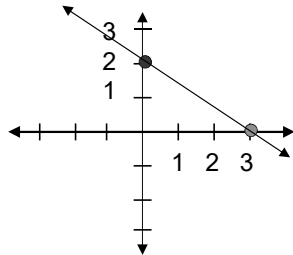
How many numbers are there between any 2 integers?.

What would happen to our graph if we used every possible value of 'x' as an input value into the function?

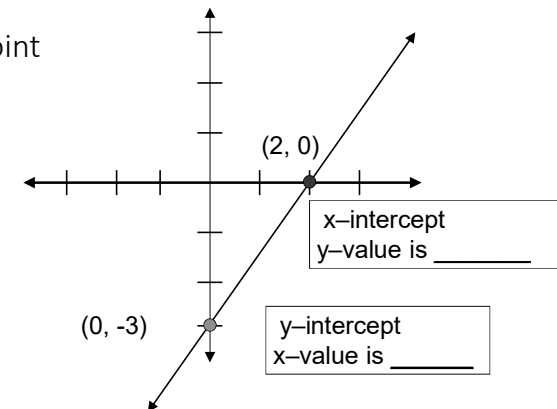
More and more points are plotted.



1. What are the coordinates [(x, y) pair] of the x-intercept?
2. What are the coordinates [(x, y) pair] of the y-intercept?
3. What is the y-coordinate of the x-intercept?
4. What is the x-coordinate of the y-intercept?

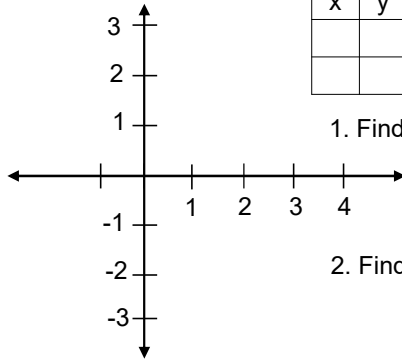


Key Point



Standard form of a linear equation: An equation
Of the form: $Ax + By = C$. Example: $3x + 4y = 12$

Graphing Standard form equations.



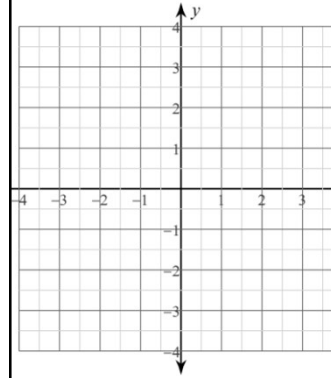
x	y	Ordered Pair

1. Find the y-intercept (let $x = 0$)

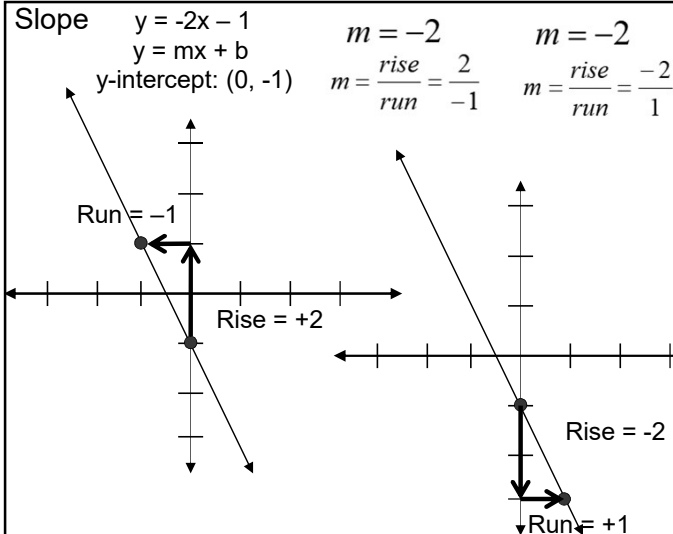
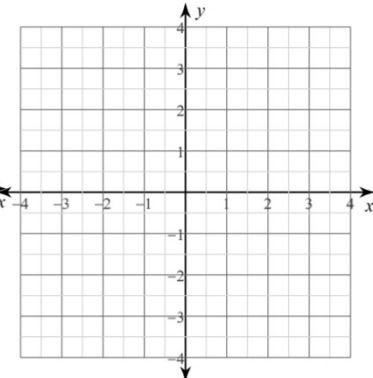
2. Find the x-intercept (let $y = 0$)

Graph the lines.

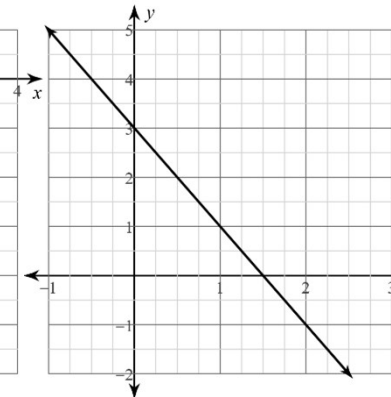
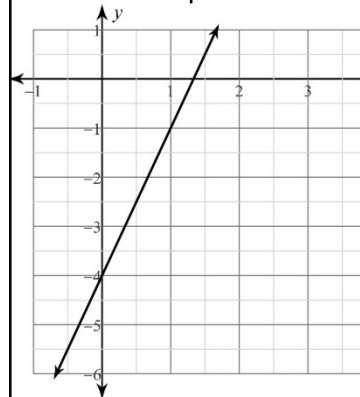
$$2x + 3y = 6$$



$$-4x + 2y = 8$$

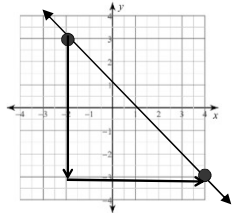


What is the equation of the line?



Find the equation of a line that passes through 2 points.

$(-2, 3)$ and $(4, -3)$



negative slope!

Rise = -6

Run = 6

$$m = \frac{\text{rise}}{\text{run}} = \frac{-6}{6} = -1$$

$$y = (-1)x + b$$

Pick either point and substitute for x and y in the equation:

$$(3) = (-1)(-2) + b$$

Solve for 'b' (the y-intercept)

$$(3) = 2 + b$$

$$-2 \quad -2$$

$$1 = b$$

$$y = -x + 1$$

Find the equation of a line that passes through 2 points.

$(3, -1)$ and $(-2, 2)$

What is the slope and y-intercept of the following equation?

$$2x - 3y = 6$$

Convert the following equation to "slope intercept form"

Re-write slope intercept form as standard form

$$y = 2x + 2 \quad \text{Slope-intercept} \rightarrow \text{standard form}$$

Parallel \rightarrow same slope $y = mx + b$

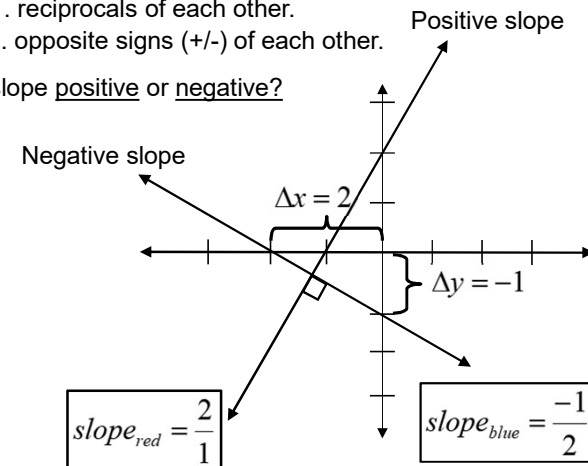
Write the equation of a line that is parallel to the line $y = 2x + 1$ and passes through the point (0, 4)

Write the equation of a line that is parallel to the line $y = 3x - 4$ and passes through the point (3, 8)

slopes of perpendicular lines are

1. reciprocals of each other.
2. opposite signs (+/-) of each other.

Is the slope positive or negative?



What two things do we know about the slopes of perpendicular lines?

The slopes of perpendicular lines are
of each other.

What is the slope a line that is perpendicular to each of the following?

$$y = 2x + 1 \qquad y = \frac{5}{9}x + 2$$

$$y = -\frac{3}{2}x - 4 \qquad y = -\frac{1}{6}x - 7$$

Find the slope intercept form of a line that is perpendicular to the line:

$$y = 2x - 6 \text{ and passes through the point } (0, 1)$$

Find the slope intercept form of a line that is perpendicular to the line:

$$y = \frac{1}{5}x - 8 \text{ and passes through the point } (5, 2)$$