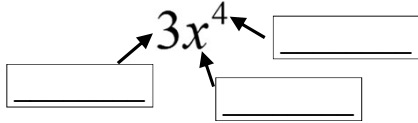


SM2 HANDOUT 2-2 (Properties of Exponents)

What is a power?

Power: An _____ formed by repeated multiplication of the _____.



The exponent applies to the number or variable _____ to its left, not to the coefficient !!!

No Exponent? $3x = 3^1 x^1$

Usually, we don't write the exponent _____ (saves ink).

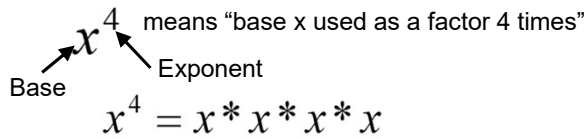
No Coefficient? $x^3 = 1 * x^3 = 1^1 * x^3$

Usually, we don't write the coefficient _____ (saves ink).

Negative? $-x^2 = (-1) * x^2 = (-1)^1 * x^2$

Usually, we don't write the coefficient '-1', we just put the " _____ " (saves ink).

Factor: a number that is being multiplied.



Power: is repeated _____ $x^4 = x * x * x * x$

multiplication: is repeated _____ $3x = x + x + x$

(adding two terms)

$3x + 4x$

$2x^2 + 3x^2$

(multiplying two terms)

$x^2 * x^3$

$$3x^2 = ?$$

There's no way to
simplify this anymore.

$$(3x)^2 = ?$$

$$4(3x)^2 = ? \text{ In GEMA, exponents occur before multiplication.}$$

$$\left(\frac{x}{2}\right)^2 = ?$$

$$\left(\frac{2}{3x}\right)^3 = ?$$

Simplify

$$(4y)^2 = ?$$

$$2(5x)^2 = ?$$

$$\left(\frac{-2}{x}\right)^4 = ?$$

$$\left(\frac{x}{2}\right)^3 = ?$$

Multiply Powers Property

$$(x^2)(x^3) = (x * x)(x * x * x)$$

This is 'x' used as a factor how many times?

$$(x^2)(x^3) = x^2 x^3 = x^{2+3} = x^5$$

'x' used as a factor five times

When you multiply powers having the
same base, you add the exponents.

Exponent of a Power Property $(x^2)^3$

$$(x^2)^3 = (x * x)(x * x)(x * x)$$

This is 'x' used as a factor how many times?

$$(x^2)^3 = x^6$$

'x' used as a factor six times

$$(x^2)^3 = x^{2*3} = x^6$$

you multiply the exponents.

Exponent of a Product Property

$$(xy)^2 = (xy)(xy) = x * y * x * y = x * x * y * y \\ = x^2 y^2$$

$$(xy)^m = x^m y^m$$

This makes it seem like you can “distribute” in the exponent. This only works with the power of a product!!

$$(x - y)^2 \neq x^2 - y^2$$

$$(x - y)^2 = (x - y)(x - y) \\ = x^2 - 2xy + y^2$$

Combination of

1. Power of a Product
2. Power of a Power

$$(3x^3 y^4)^2 = (3^1 x^3 y^4)^2 \\ = 3^2 x^6 y^8$$

Constants (integer, etc.) usually have an exponent of ‘1’.

‘x’ is a number, we just don’t know what it is. You treat all numbers the same (whether they are variables or constants).

$$3x^2(4x^3) = ? = 3 * 4 * (x^2)(x^3) = 12x^5$$

You can re-arrange the order of multiplication.

Coefficients of the powers are handled separately from the base and the exponent.

$$(x^2)^5 = ?$$

$$(5x^2)(2x^3) = ?$$

$$(2y^5)^3 = ?$$

Be careful of exponents of negative numbers

$$(-x^3 y^4)^2 \\ = ((-1)^1 x^3 y^4)^2 \text{ Turn negative signs into multiplication by -1.}$$

$$= (-1)^2 x^6 y^8 \text{ This way you will be able to tell if the simplified version is positive or negative.} \\ = x^6 y^8$$

$$(-2x^2 y^6)^3 \text{ Negative coefficients have an exponent of '1'.} \\ = ((-2)^1 x^2 y^6)^3$$

$$= (-2)^3 x^6 y^{18} \text{ A negative number raised to an odd exponent remains negative.} \\ = -8x^6 y^{18}$$

simplify

$$(-2x^2y^4z)^3$$

$$2(-m^4x^3)^5$$

$$-3(-2x^2yz^3)^4$$

$$(-2x^2y^4z)^3$$

$$-3(-2x^2yz^3)^4$$

Negative Exponent Property Possible errors

$$4x^{-2} = \frac{4 \cdot x^{-2}}{1} = \frac{4}{x^2}$$

When you "Grab and drag" the base and its exponent across the "boundary line" between numerator and denominator, you just change the sign of the exponent.

DO NOT GRAB the coefficient! $\frac{4 * x^{-2}}{1} \neq \frac{1}{4x^2}$

Zero Exponent Property

Any base raised to the zero power simplifies to one.

$$10^3 = 1000 \quad 10^2 = 100 \quad 10^1 = 10 \quad 10^0 = 1$$

$$\frac{32x^{10}}{(x^2y^{17})^4}$$

"Grab and drag" Product of powers: add the exponents of same based powers

$$\frac{3x^2}{2(x^{-4})y}$$

Do you "grab and drag (up or down)??"

$$\frac{3x^2}{2x^{-4}y}$$

It doesn't matter!!!!

$$\left(\frac{x^2}{x^4}\right)^2$$

$$\left(\frac{yx^3}{xz}\right)^4$$

$$\left(\frac{3x^0}{2x^{-1}y}\right)^2$$

$$\left(\frac{2x^2yz^{-2}}{6x^4y^3z^3}\right)^2$$