## Math-2A Lesson 4-8 <br> Applications of Linear Equations

Quantity: A category of measurement of a real world physical property (length, width, temperature, pressure, weight, etc.).

Unit of Measure: How the quantity is measured (inches, feet, square feet, etc.

$$
\text { Area } a_{\mathrm{rectangle}}=l * w
$$



Perimeter ${ }_{\text {rectangle }}=2 L+2 w$
Area $a_{\text {triangle }}=\frac{1}{2} b h$


| Time (min) | 0 | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Height (ft) | 36,000 | 32,000 | 28,000 | 24,000 | 20,000 |

(The table shows the altitude of an airplane.) write equation: $y=m x+b$
$\rightarrow$ what is the slope? $\quad m=\frac{\text { rise }}{\text { run }} \quad=\frac{-4000 \mathrm{ft}}{\min }$
What is the $y$-intercept ?
$(0, b) \quad(0,36000)$
$y=-4000 x+36000$
TEST your equation. $\quad 32,000=-4,000(1)+36,000$
Equation is "true"

| Time <br> $(\mathrm{min})$ | $8: 03 \mathrm{AM}$ | 8:04 AM | 8:05 AM | 8:06 AM | 8:07 AM |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Height <br> (ft) | 36,000 | 32,800 | 29,600 | 26,400 | 23,200 |

Notice how this date doesn't start at zero.
To write an equation, you need a y-intercept.
It is often easier to change the time to read "time since" some reference point.

| Time (min) <br> (since 8:03 AM) | 0 | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Height (ft) | 36,000 | 32,800 | 29,600 | 26,400 | 23,200 |


| Year | 1990 | 1992 | 1994 | 1996 | 1998 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Imports <br> (Billions \$) | 52 | 55 | 58 | 61 | 64 |

(This table shows imports for various years.) write equation: $y=m x+b$
$\rightarrow$ what is the slope?
Rise $=$ \$55B - \$52B $=\$ 3 \mathrm{~B}$

$$
m=\frac{\text { rise }}{r u n}=\frac{\$ 3 \mathrm{~B}}{2 \mathrm{yrs}}
$$

$$
\text { Run }=1992-1990=2 \text { years }
$$

What is the $y$-intercept ? $\rightarrow(0, b)$

$$
m=\frac{\$ 1.5 \mathrm{~B}}{\mathrm{yrs}}
$$

The year "zero" ??!!
Change year to "years since 1990")

| Yrs. Since <br> 1990 | 0 | 2 | 4 | 6 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Imports <br> (Billions \$) | 52 | 55 | 58 | 61 | 64 |

(This table shows imports for various years.)
write equation: $y=m x+b$
$\rightarrow$ what is the slope?
Rise $=\$ 55 \mathrm{~B}-\$ 52 \mathrm{~B}=\$ 3 \mathrm{~B}$

$$
m=\frac{\text { rise }}{r u n}=\frac{\$ 3 \mathrm{~B}}{2 \mathrm{yrs}}
$$

$$
\text { Run }=1992-1990=2 \text { years }
$$

What is the $y$-intercept ? $\rightarrow(0, b)$

$$
m=\frac{\$ 1.5 \mathrm{~B}}{\mathrm{yrs}}
$$

$$
\begin{aligned}
& b=\$ 52 B \\
& y=1.5 x+52
\end{aligned}
$$

What is the equation of the line that can represent this data?

| Time (min) | 0 | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Height (ft) | 500 | 450 | 400 | 350 | 300 |


| Year | 1900 | 1910 | 1920 | 1930 | 1940 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Population <br> (millions) | 100 | 125 | 150 | 175 | 200 |


| Yrs since <br> 1900 | 0 | 10 | 20 | 30 | 40 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Population <br> (millions) | 100 | 125 | 150 | 175 | 200 |

What is the equation of the line that can represent this data?

| Time | 11 AM | $11: 30$ <br> AM | 12 PM | $12: 30$ <br> PM | 1 PM |
| :---: | :---: | :---: | :---: | :---: | :---: |
| distance <br> (miles) | 50 | 75 | 100 | 125 | 150 |


| Time (since <br> 11 AM) (hrs) | 0 | 0.5 | 1 | 1.5 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| distance <br> (miles) | 50 | 75 | 100 | 125 | 150 |

Find the equation that "models" the data.

| Time (yrs) | 1987 | 1991 | 1995 | 1999 | 2003 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Trade deficit <br> (Billions of \$'s) | 36.0 | 32.8 | 29.6 | 26.4 | 23.2 |



Write the equation: $y=m x+b$
Slope: $\quad(0,20) \rightarrow(8,80)$

$$
\begin{gathered}
m=\frac{\text { rise }}{r u n}=\frac{60 \mathrm{miles}}{8 \mathrm{hrs}} \\
m=7.5 \frac{\mathrm{miles}}{\mathrm{hr}}
\end{gathered}
$$

$$
y=7.5 x+20
$$

Your parents are paying "big bucks" for your health club membership. You go to the health club 4 days/week. The time it takes to walk/run 3 miles at the end of each week has been graphed. Write an equation for the relation.

$$
y=m x+b
$$

Slope: $\quad(0,44) \rightarrow(8,36)$

| 44 下 | rise $\quad-8 \mathrm{~min}$ |
| :---: | :---: |
| $\begin{aligned} & 42 \text { 十 } \\ & 40 \end{aligned}$ | $m=\frac{r s}{r u n}=\frac{8 \text { weeks }}{8 \text { min }}$ |
| 38 |  |
| ¢. ${ }_{\text {¢ }}{ }^{36}$ 34- | $m=-1 \frac{\mathrm{~min}}{m}$ |
|  | wk |
|  | $y=-x+44$ |
| 12345678 |  |
| Time (weeks) |  |

During the first 5 weeks of your exercise program you record your weight.

| End of <br> Week, $w$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| weight, $y$ <br> (lb.) | 186 | 183 | 180 | 177 | 174 | 171 |

Determine the average rate of change of your weight during the 5 -week period.

Assuming your weight loss will continue at the same rate, write an equation that relates your weight to the number of weeks on the exercise program.

You decide to buy a new Honda Civic, but you are concerned about the value of the car depreciating over time. You search the Internet and obtain the following information.

## Suggested Retail Price: \$20,905

Depreciation per year: $\$ 1750$ (assume constant)

1) What does this mean?
2) Complete the table.
" V " is the value of the car after " n " years of ownership

| n (years) | $\mathbf{0}$ | $\mathbf{1}$ | 2 | 3 | 5 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~V},(\$)$ | 20,905 | 19,155 | 17405 | 15,655 | 12,155 | 6905 |

3) Write the equation that predicts the value of the car based upon its age in the year.

A car rental company charges: $\$ 60$ per day plus $\$ 0.75$ per mile Fill in the remainder of the table.

Write the equation that predicts the cost of renting the car based upon how many miles are driven.

$$
C_{A}(m)=0.75 m+60
$$

| $" m "$ <br> miles | Total <br> Cost |
| :---: | :---: |
| 0 |  |
| 50 |  |
| 100 |  |
| 150 |  |
| 200 |  |
| 250 |  |
| 300 |  |

How much would your bill be if you drove the car 525 miles?

## Hamburgers cost $\$ 5$ and drinks cost $\$ 2$.

If you can spend a total of $\$ 50$, fill in the total number of hamburgers and drinks that you can buy.

| Hamburgers | drinks |
| :---: | :--- |
| 0 |  |
| 2 |  |
| 4 |  |
| 6 |  |
| 8 |  |
| 10 |  |

Write and equation for this table.

$$
D=\frac{-5}{2} H+25
$$

