

SM2 HANDOUT 5-6 (Quadratic Modeling: Area)

Quantity	Unit of Measure
Height	
Weight	
Temperature	

Sometimes ratios of quantities become new quantities

Quantity	Ratio of:	Unit of Measure
Speed	Distance/time	
"unit price"	Cost/weight	

Vocabulary

Mathematical Modeling: representing a real-world phenomenon or quantity with an equation or inequality.

Formula: an equation that shows the relationship between two or more quantities.

Examples of formulas you've seen are:

$$A_{circle} = \pi r^2 \qquad V_{box} = L * w * h$$

$$A_{rectangle} = L * W \qquad A = \frac{1}{2}(b_1 + b_2)h$$

Expressions from Phrases

What mathematical expression represents the following?

Three more than twice a number

Five less than three times a number

The width is 4 times the length.

The area of a rectangle whose width is 4 times its length.

Write a mathematical expression that represent each statement:

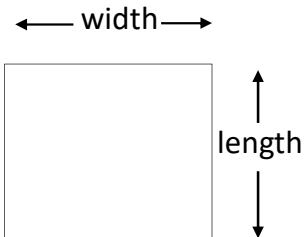
1. The number of girls is three less than twice the number of boys.

2. The salary after a 4% increase

3. Area of a rectangle whose length is 2 more than twice its width.

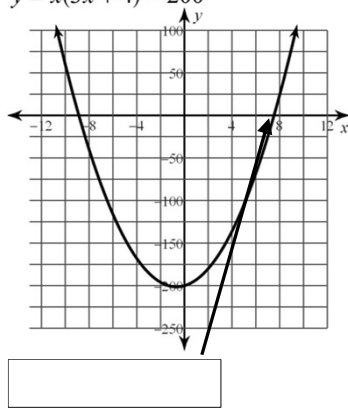
4. The area of a rectangle with the same size square cut out of each corner.

Area of a Rectangle  
 The length of a rectangle is 4 more than 3 times its width.  
 The area of the rectangle is 200 square inches.  
 What is the length and width of the rectangle?  
 Area =  $L * W$   
 $L = 3W + 4$      $A = 200$   
 Using substitution:  
 $200 = (3W + 4) * W$   
 Solve by graphing.



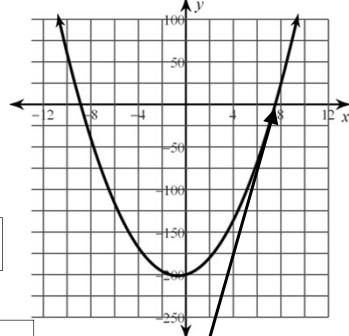
Area of a Rectangle  
 Area =  $L * W$   
 $L = 3W + 4$      $A = 200$   
 Using substitution:  
 $200 = (3W + 4) * W$   
 Solve by graphing.  
 Get into "zero equals form"  
 $0 = W(3W + 4) - 200$   
 Let 'x' = width  
 $0 = x(3x + 4) - 200$

$y = x(3x + 4) - 200$   
 Find the "zero" of the equation.  
 $y = x(3x + 4) - 200$



Area of a Rectangle  
 Area =  $L * W$   
 $L = 3W + 4$      $A = 200$   
 Using substitution:  
 $200 = (3W + 4) * W$   
 $y = x(3x + 4) - 200$   
 Using substitution:  
 $L = 3W + 4$

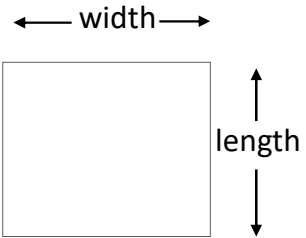
Find the "zero" of the equation.  
 $y = x(3x + 4) - 200$



Check:  $200 = L * W$     Check:  $200 = \underline{\hspace{2cm}}$      $W = \underline{\hspace{2cm}}$

Area of a Rectangle  
 The length of a rectangle is 7 less than 4 times its width.  
 The area of the rectangle is 6600 square inches.  
 What is the length and width of the rectangle?  
 Area =  $\underline{\hspace{2cm}} * \underline{\hspace{2cm}}$   
 $L = \underline{\hspace{2cm}}$      $A = \underline{\hspace{2cm}}$

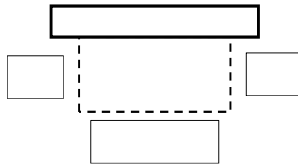
Using substitution:  
 $\underline{\hspace{2cm}} = (\underline{\hspace{2cm}}) * \underline{\hspace{2cm}}$   
 Solve by graphing.



Area of a Rectangle

200 feet of fence is used to build a rectangular horse corral. One side of the corral is next to a large barn and does not need to be fence.

a) Draw a top-view picture of the corral and barn.



b) Label the length of each side of a fenced corral using only one variable.

c) Using the rectangle area formula, write an equation that has only one variable.

$A(x) =$

d) What are the x-intercepts?

e) What is the vertex?

f) Hand-draw a graph of the equation with the axes correctly labeled.

g) Graph the equation on your calculator, and find the vertex using "2<sup>nd</sup>" + "calc" + "maximum"

