Math-1010 Final Exam Review #2

Identify the domain and range of each.

1)
$$y = \log_5 (2x - 1) - 2$$

Domain: $x > \frac{1}{2}$

Range: All reals

2)
$$y = \log_2 (4x + 10)$$

Domain: $x > -\frac{5}{2}$

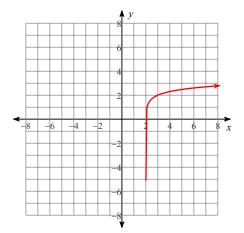
Range: All reals

Evaluate each expression.

3)
$$\log_6 \frac{1}{36}$$

Sketch the graph of each function.

4)
$$y = \log(x-2) + 2$$



Rewrite each equation in exponential form.

5)
$$\log_{14} \frac{1}{196} = -2 \quad 14^{-2} = \frac{1}{196}$$

Rewrite each equation in logarithmic form.

6)
$$\left(\frac{1}{7}\right)^3 = \frac{1}{343}$$

$$\log_{\frac{1}{7}} \frac{1}{343} = 3$$

Find the inverse of each function.

7)
$$y = \log_6(x+1)$$

 $y = 6^x - 1$

8)
$$y = 3 \cdot 2^{x} + 4$$

 $y = \log_{2} \left(\frac{x}{3} - 4 \right)$

9)
$$y = 2 \cdot \left(\frac{1}{3}\right)^x - 1$$

$$y = \log_{\frac{1}{3}} \frac{x+1}{2}$$

Perform the indicated operation.

10)
$$h(t) = t^3 + 4t$$

 $g(t) = 3t - 2$
Find $(h \cdot g)(t)$
 $3t^4 - 2t^3 + 12t^2 - 8t$

11)
$$g(n) = 3n - 1$$

 $f(n) = 4n + 3$
Find $(g \circ f)(n)$
 $12n + 8$

12)
$$f(x) = x^3 + 5$$

 $g(x) = 3x + 1$
Find $(3f + 5g)(x)$
 $3x^3 + 15x + 20$

13)
$$g(x) = -2x + 4$$

 $h(x) = x^2 - 2$
Find $(g \cdot h)(-3)$

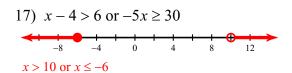
14)
$$h(a) = a^2 - 2$$

 $g(a) = 2a + 4$
Find $(-3h + 5g)(-2)$

15)
$$h(n) = 2n^2 + 2 + 2n$$

 $g(n) = n + 3$
Find $(h \circ g)(-6)$

Simplify the inequality then graph its solution.



Solve each equation by completing the square.

18)
$$0 = x^2 - 6x - 38$$

 $\{3 + \sqrt{47}, 3 - \sqrt{47}\}$

19)
$$0 = x^2 + 14x + 1$$

-7 + $4\sqrt{3}$, -7 - $4\sqrt{3}$

Solve each equation by factoring.

20)
$$2m^2 + 3m = 0$$
 $\left\{-\frac{3}{2}, 0\right\}$

21)
$$3k^2 - 14k + 15 = 0$$
 $\left\{\frac{5}{3}, 3\right\}$

Solve each equation by taking square roots.

22)
$$3k^2 + 6 = 102$$
 $\left\{4\sqrt{2}, -4\sqrt{2}\right\}$

23)
$$16n^2 - 3 = 97 \quad \left\{ \frac{5}{2}, -\frac{5}{2} \right\}$$

- 24) For the following data: (0,3), (1, 3.6), (2, 4.32), (3, 5.184) a) $y = 3 \cdot 1.2^{x}$
 - b) b = 1.2

a) What is the equation that fits the data?

c) 20%

- b) What is the growth factor?
- c) What is the percent rate of change?
- 25) For the following data: (0,5), (1, 4.25), (2, a) $y = 5 \cdot 0.85^{x}$ 3.1625) b) b = 0.85c) -15%
 - a) What is the equation that fits the data?
 - b) What is the growth factor?
 - c) What is the percent rate of change?
- 26) A basketball is thrown upward from the top of a 75 foot building. The equation that models the position of the ball (height above ground level in feet) and the ball's horizontal distance traveled (x feet) is: $h \cdot x = -0.5x^2 + 4x + 75$

How far away from the build must a basketball hoop be place so that the ball, when thrown will pass through the basket. The height of the basketball hoop is 10 feet above the ground.

16.1 ft